Unit 8, Lesson 11

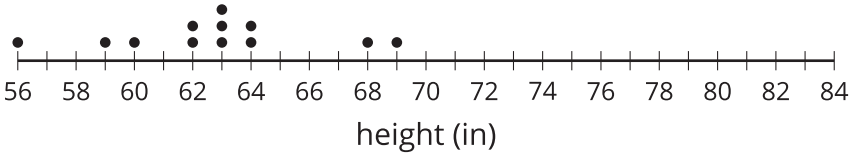
Comparing Groups

Let's compare two groups.

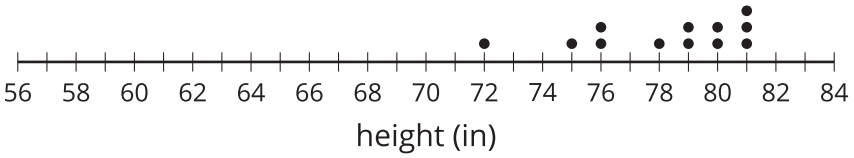
11.1 Notice and Wonder: Comparing Heights

What do you notice? What do you wonder?

gymnastics team



volleyball team



11.2 More Team Heights

1. How much taller is the volleyball team than the gymnastics team?
   - Gymnastics team's heights (in inches): 56, 59, 60, 62, 62, 63, 63, 63, 64, 64, 68, 69
   - Volleyball team's heights (in inches): 72, 75, 76, 76, 78, 79, 79, 80, 80, 81, 81, 81

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2. Make dot plots to compare the heights of the tennis and badminton teams.
    - Tennis team's heights (in inches): 66, 67, 69, 70, 71, 73, 73, 74, 75, 75, 76
    - Badminton team's heights (in inches): 62, 62, 65, 66, 68, 71, 73

What do you notice about your dot plots?

3. Elena says the members of the tennis team are taller than the badminton team. Lin disagrees. Do you agree with either of them? Explain or show your reasoning.

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11.3 Family Heights

Compare the heights of these two families. Explain or show your reasoning.

- The heights (in inches) of Noah's family members: 28, 39, 41, 52, 63, 66, 71
- The heights (in inches) of Jada's family members: 49, 60, 68, 70, 71, 73, 77

Are you ready for more?

If Jada's family adopts newborn twins who are each 18 inches tall, does this change your thinking? Explain your reasoning.

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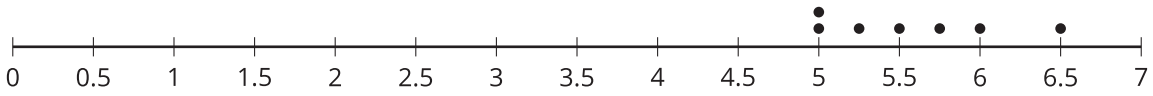
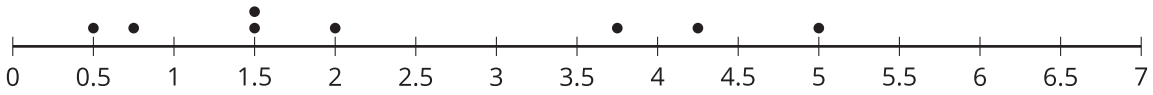
11.4 Track Length

Here are three dot plots that represent the lengths, in minutes, of songs on different albums.

A



B



C



1. One of these data sets has a mean of 5.57 minutes and another has a mean of 3.91 minutes.
   a. Which dot plot shows each of these data sets?

   b. Calculate the mean for the data set on the other dot plot.

2. One of these data sets has a mean absolute deviation (MAD) of 0.30, and another has a MAD of 0.44.
   a. Which dot plot shows each of these data sets?

   b. Calculate the MAD for the other data set.

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3. Do you think the three groups are very different or not? Be prepared to explain your reasoning.

4. A fourth album has a mean length of 8 minutes with a mean absolute deviation of 1.2. Is this data set very different from each of the others?

Lesson 11 Summary

Comparing two individuals is fairly straightforward. The question, "Which dog is taller?" can be answered by measuring the heights of two dogs and comparing them directly. Comparing two groups can be more challenging. What does it mean for beagle dogs to generally be taller than pug dogs?

To compare two groups, we use the distribution of values for the two groups. Most importantly, a measure of center (usually **mean** or **median**) and its associated measure of variability (usually **mean absolute deviation** or **interquartile range**) can help determine the differences between groups.

For example, if the average height of pugs in a dog show is 11 inches, and the average height of the beagles in the dog show is 15 inches, it seems that the beagles are generally taller. On the other hand, if the mean absolute deviation (MAD) is 3 inches, it would not be unreasonable to find a beagle that is 11 inches tall or a pug that is 14 inches tall. Therefore the heights of the two dog breeds may not be very different from one another.