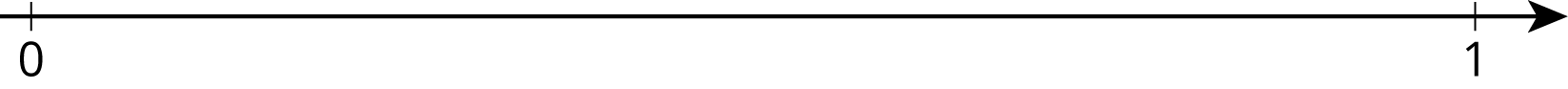
## Unit 8 Lesson 4: Estimating Probabilities Through Repeated Experiments

### 1 Decimals on the Number Line (Warm up)

#### Student Task Statement

1. Locate and label these numbers on the number line.
   1. 0.5
   2. 0.75
   3. 0.33
   4. 0.67
   5. 0.25

* 

1. Choose one of the numbers from the previous question. Describe a game in which that number represents your probability of winning.

### 2 In the Long Run

#### Images for Launch

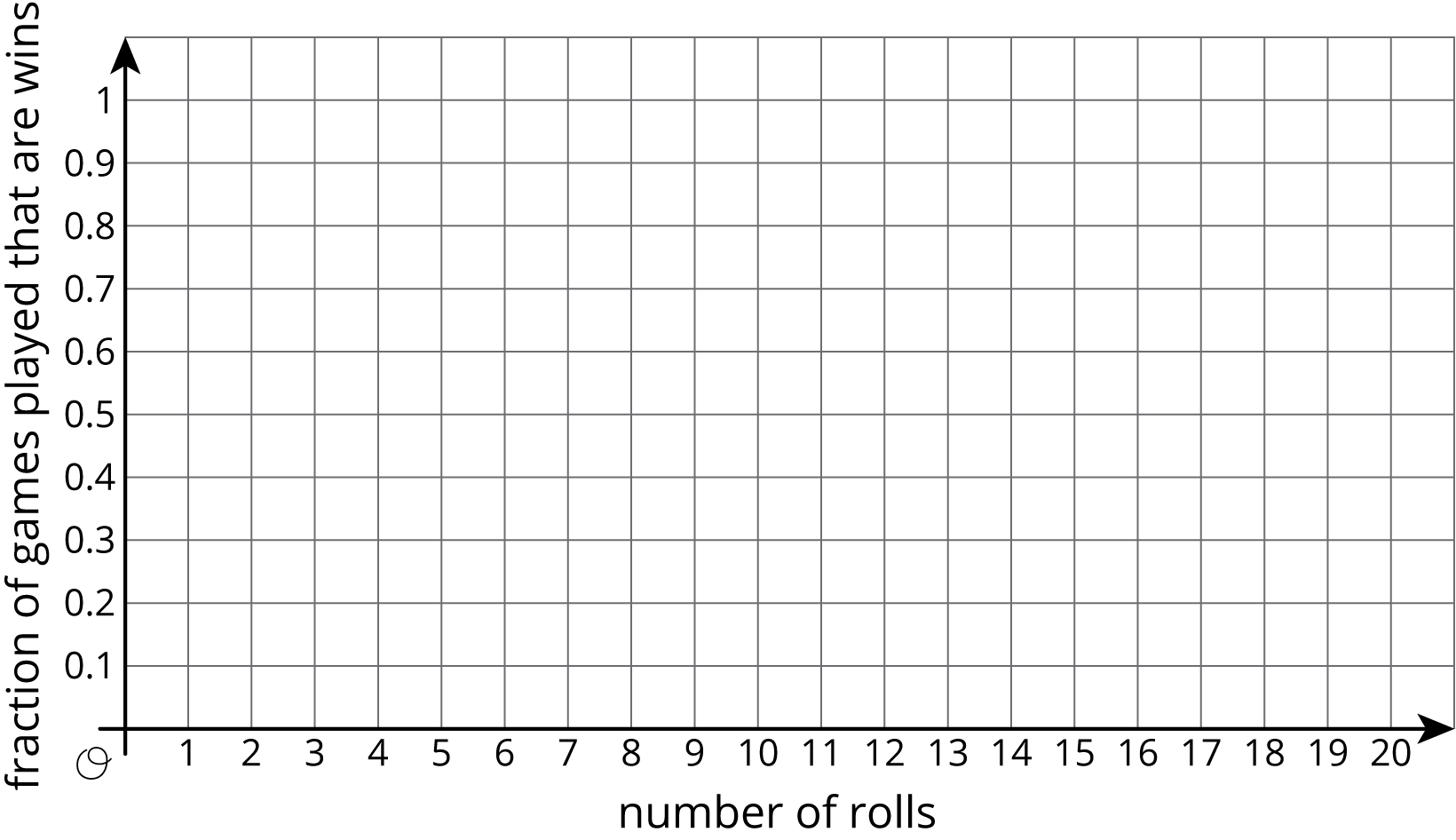


#### Student Task Statement

Mai plays a game in which she only wins if she rolls a 1 or a 2 with a standard number cube.

1. List the outcomes in the sample space for rolling the number cube.
2. What is the probability Mai will win the game? Explain your reasoning.
3. If Mai is given the option to flip a coin and win if it comes up heads, is that a better option for her to win?
4. With your group, follow these instructions 10 times to create the graph.
   * One person rolls the number cube. Everyone records the outcome.
   * Calculate the fraction of rolls that are a win for Mai so far. Approximate the fraction with a decimal value rounded to the hundredths place. Record both the fraction and the decimal in the last column of the table.
   * On the graph, plot the number of rolls and the fraction that were wins.
   * Pass the number cube to the next person in the group.

| * roll | * outcome | * total number of wins for Mai | * fraction of games played that are wins |
| --- | --- | --- | --- |
| * 1 |  |  |  |
| * 2 |  |  |  |
| * 3 |  |  |  |
| * 4 |  |  |  |
| * 5 |  |  |  |
| * 6 |  |  |  |
| * 7 |  |  |  |
| * 8 |  |  |  |
| * 9 |  |  |  |
| * 10 |  |  |  |

* 

1. What appears to be happening with the points on the graph?
   1. After 10 rolls, what fraction of the total rolls were a win?
   2. How close is this fraction to the probability that Mai will win?
2. Roll the number cube 10 more times. Record your results in this table and on the graph from earlier.

| * roll | * outcome | * total number of wins for Mai | * fraction of games played that are wins |
| --- | --- | --- | --- |
| * 11 |  |  |  |
| * 12 |  |  |  |
| * 13 |  |  |  |
| * 14 |  |  |  |
| * 15 |  |  |  |
| * 16 |  |  |  |
| * 17 |  |  |  |
| * 18 |  |  |  |
| * 19 |  |  |  |
| * 20 |  |  |  |

* 1. After 20 rolls, what fraction of the total rolls were a win?
  2. How close is this fraction to the probability that Mai will win?

### 3 Due For a Win

#### Student Task Statement

1. For each situation, do you think the result is surprising or not? Is it possible? Be prepared to explain your reasoning.
   1. You flip the coin once, and it lands heads up.
   2. You flip the coin twice, and it lands heads up both times.
   3. You flip the coin 100 times, and it lands heads up all 100 times.
2. If you flip the coin 100 times, how many times would you expect the coin to land heads up? Explain your reasoning.
3. If you flip the coin 100 times, what are some other results that would not be surprising?
4. You’ve flipped the coin 3 times, and it has come up heads once. The cumulative fraction of heads is currently . If you flip the coin one more time, will it land heads up to make the cumulative fraction ?



© CC BY Open Up Resources. Adaptations CC BY IM.