

# Lesson 1: Properties of Exponents

- Let's use integer exponents.

## 1.1: Which One Doesn't Belong: Exponents and Equations

- A.  $2^3 = 9$
- B.  $9 = 3^2$
- C.  $2 \cdot 2 \cdot 2 \cdot 2 = 16$
- D.  $a \cdot 2^0 = a$

## 1.2: Name That Power

Find the value of each variable that makes the equation true. Be prepared to explain your reasoning.

1.  $2^3 \cdot 2^5 = 2^a$

2.  $3^b \cdot 3^7 = 3^{11}$

3.  $\frac{4^3}{4^2} = 4^c$

4.  $\frac{5^8}{5^d} = 5^2$

5.  $6^m \cdot 6^m \cdot 6^m = 6^{21}$

6.  $(7^n)^4 = 7^{20}$

7.  $2^4 \cdot 3^4 = 6^s$

8.  $5^3 \cdot t^3 = 50^3$

### 1.3: The Power of Zero

1. Use exponent rules to write each expression as a single power of 2. Find the value of the expression. Record these in the table. The first row is done for you.

expression	power of 2	value
$\frac{2^5}{2^1}$	$2^4$	16
$\frac{2^5}{2^2}$		
$\frac{2^5}{2^3}$		
$\frac{2^5}{2^4}$		
$\frac{2^5}{2^5}$		
$\frac{2^5}{2^6}$		
$\frac{2^5}{2^7}$		

2. What is the value of  $5^0$ ?

3. What is the value of  $3^{-1}$ ?

4. What is the value of  $7^{-3}$ ?

#### Are you ready for more?

Explain why the argument used to assign a value to the expression  $2^0$  does not apply to make sense of the expression  $0^0$ .

## 1.4: Matching Exponent Expressions

Sort expressions that are equal into groups. Some expressions may not have a match, and some may have more than one match. Be prepared to explain your reasoning.

$$\begin{array}{cccccccc}
 2^{-4} & \frac{1}{2^4} & -2^4 & -\frac{1}{2^4} & 4^2 & 4^{-2} & -4^2 & -4^{-2} \\
 2^7 \cdot 2^{-3} & \frac{2^7}{2^{-3}} & 2^{-7} \cdot 2^3 & \frac{2^{-7}}{2^{-3}} & (-4)^2 & & & 
 \end{array}$$

### Lesson 1 Summary

Exponent rules help us keep track of a base's repeated factors. Negative exponents help us keep track of repeated factors that are the *reciprocal* of the base. We can define a number to the power of 0 to have a value of 1. These rules can be written symbolically as:

$$\begin{aligned}
 b^m \cdot b^n &= b^{m+n} \\
 (b^m)^n &= b^{m \cdot n} \\
 \frac{b^m}{b^n} &= b^{m-n} \\
 b^{-n} &= \frac{1}{b^n} \\
 b^0 &= 1 \\
 a^n \cdot b^n &= (a \cdot b)^n
 \end{aligned}$$

Here, the base  $b$  can be any positive number, and the exponents  $n$  and  $m$  can be any integer.