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Finding Intersections

Let's think about two polynomials at once.

11.1

Math Talk: When f Meets g

Find a point mentally where the graphs of the two functions intersect, if one exists.

•
$$f(x) = x$$
 and $g(x) = 3$

•
$$j(x) = (x+3)(x-3)$$
 and $k(x) = 0$

•
$$m(x) = (x+3)(x-3)$$
 and $n(x) = (x-3)$

•
$$p(x) = (x+5)(x-5)$$
 and $q(x) = (x+3)(x-3)$



11.2

More Points of Intersection

For each pair of polynomials given, find all points of intersection of their graphs.

1.
$$c(x) = x^2 - 7$$
 and $d(x) = 2$

2.
$$f(x) = (x+7)(x-4)$$
 and $g(x) = x-4$

3.
$$m(x) = (x + 7)(x - 4)$$
 and $n(x) = (2x + 5)(x - 4)$

4.
$$p(x) = (x + 1)(x - 8)$$
 and $q(x) = (x + 2)(x - 4)$



Are you ready for more?

Find all points of intersection of the graphs of the equations p(x) = (2x + 3)(x - 5) and q(x) = (x + 5)(x + 1)(x - 3). Use graphing technology to check your solutions.

11.3

Graphing to Find Points of Intersection

Consider the functions $p(x) = 5x^3 + 6x^2 + 4x$ and q(x) = 5640.

- 1. Use graphing technology to find a value of x that makes p(x) = q(x) true.
- 2. Using the *x*-value at the point of intersection, what is the value of $5x^3 + 6x^2 + 4x 5640$?
- 3. What does your answer suggest is a possible factor of $5x^3 + 6x^2 + 4x 5640$?
- 4. a. Write your own polynomial m(x) of degree 3 or higher.

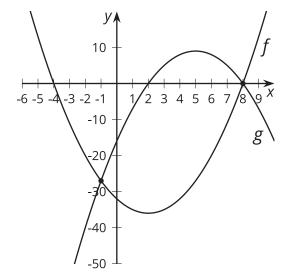
b. Use graphing technology to estimate the values of x that make m(x)=q(x) true.



Lesson 11 Summary

When asked to find all values of x that make an equation like (x + 4)(x - 8) = (2 - x)(x - 8)true, one way to consider the question is to ask where the graphs of the functions

$$f(x) = (x + 4)(x - 8)$$
 and $g(x) = (2 - x)(x - 8)$ intersect.



Since the coordinate of any point of intersection has the form (a, f(a)) = (a, g(a)), these points must make f(x) = g(x) true when x = a. In our example, we can tell from the graph that both x = -1 and x = 8 are solutions to the original equation.

We can also use algebra to identify solutions to (x + 4)(x - 8) = (2 - x)(x - 8) by rearranging and then recognizing that both parts have a factor of (x - 8) in common:

$$(x+4)(x-8) = (2-x)(x-8)$$

$$(x+4)(x-8) - (2-x)(x-8) = 0$$

$$(x-8)(x+4-2+x) = 0$$

$$(x-8)(2x+2) = 0$$

$$x = 8,-1$$

For polynomials created to model specific situations that have a more complicated structure, solving without using technology can be challenging, especially because the graphs of two polynomials can intersect at multiple points.

