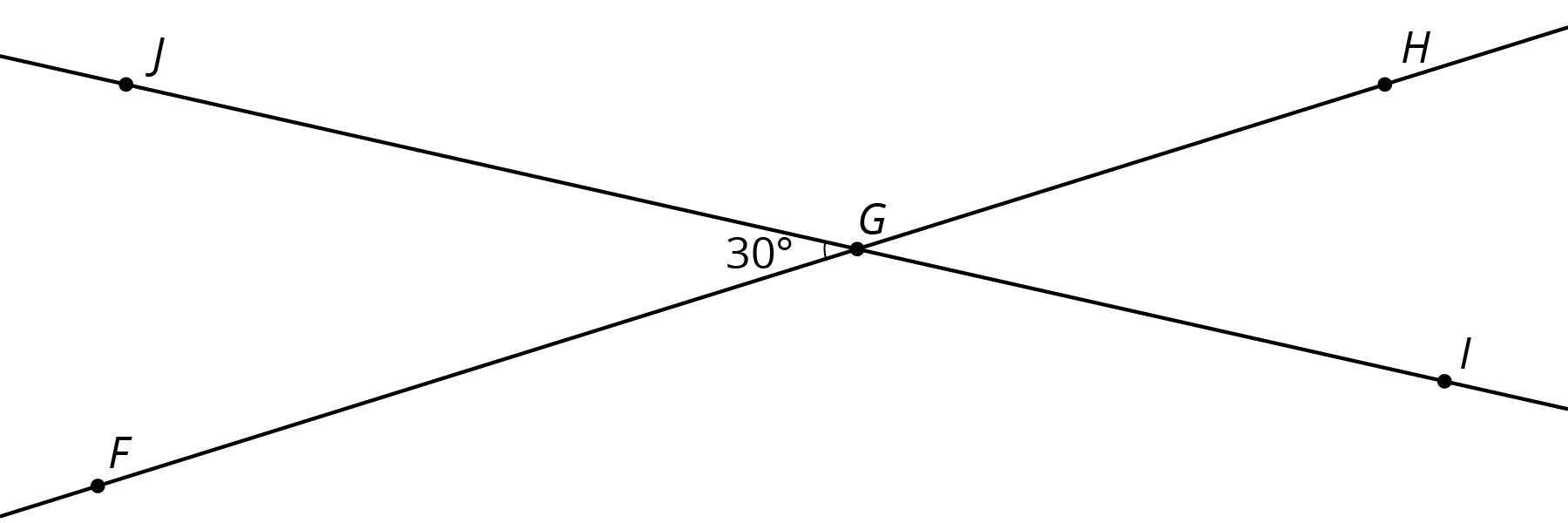
## Lesson 12: Alternate Interior Angles

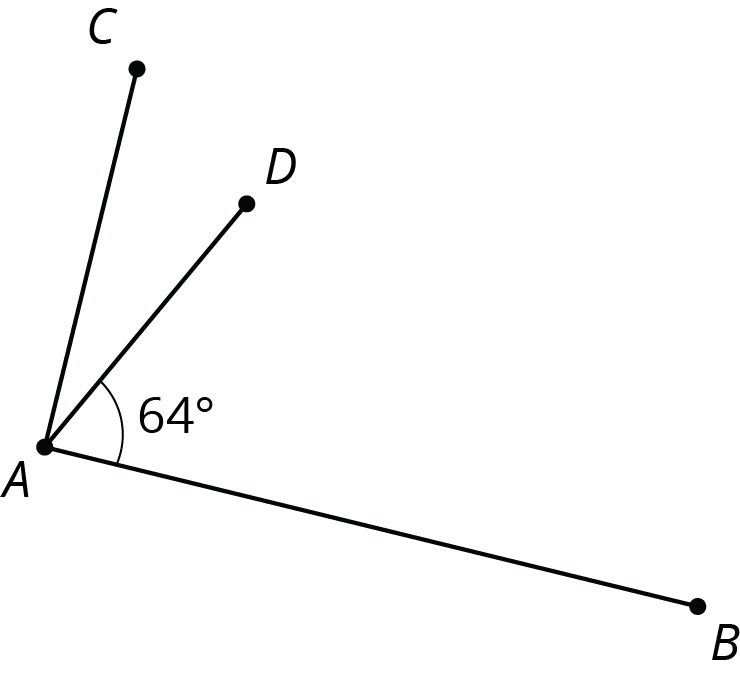
Let’s explore why some angles are always equal.

### 12.1: Angle Pairs

1. Find the measure of angle . Explain or show your reasoning.

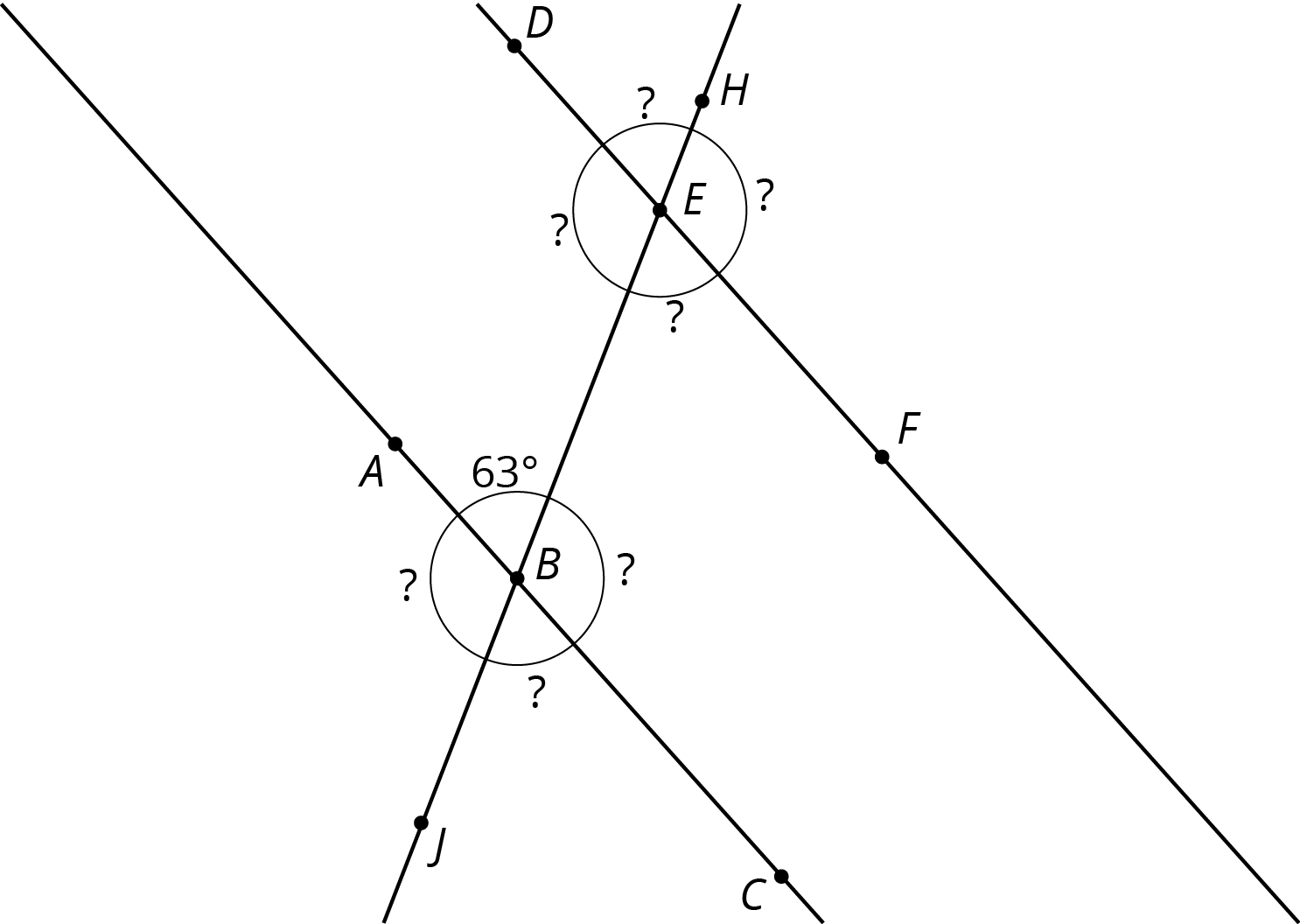
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1. Find and label a second angle in the diagram. Find and label an angle congruent to angle .
2. Angle is a right angle. Find the measure of angle .

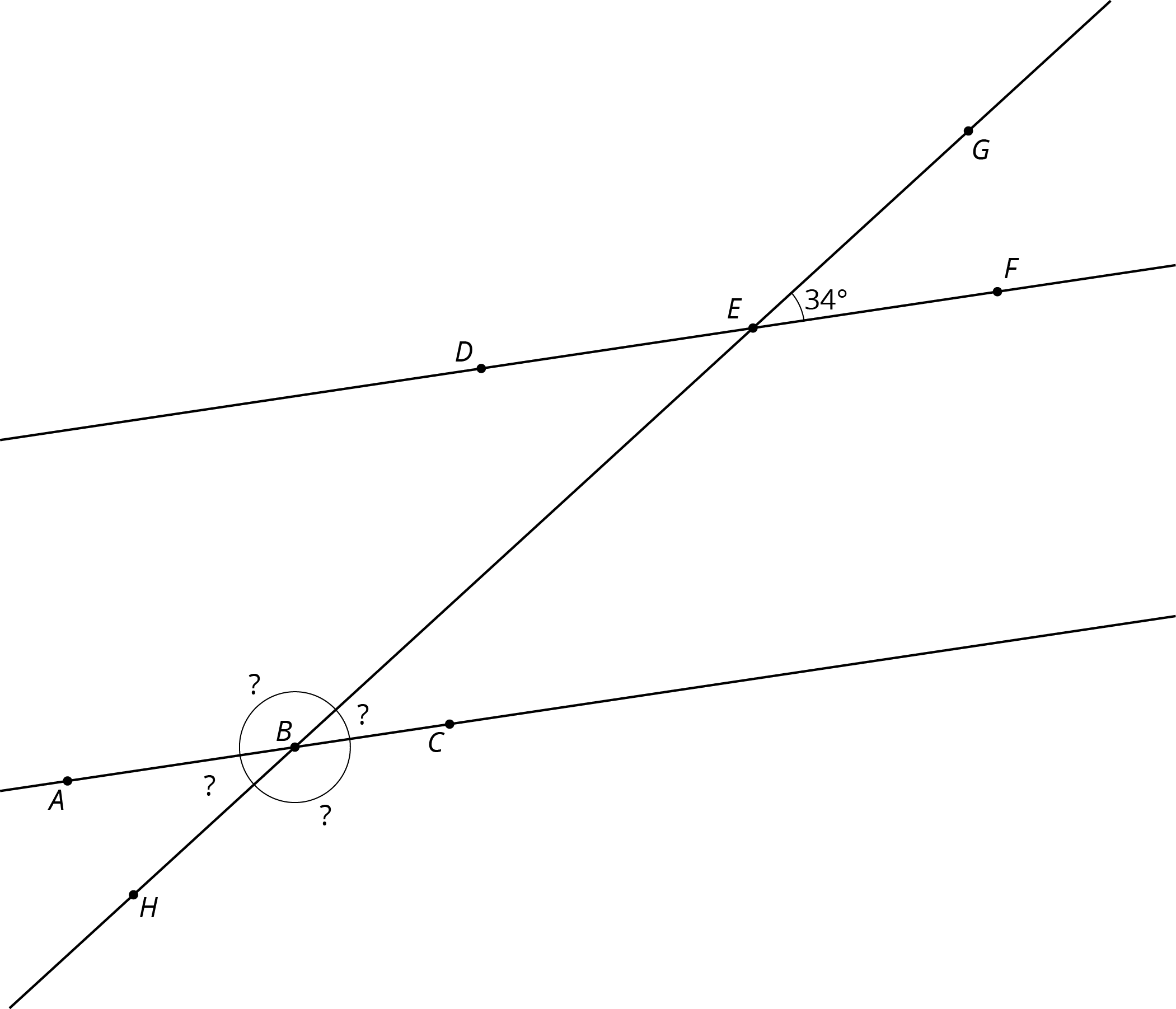
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### 12.2: Cutting Parallel Lines with a Transversal

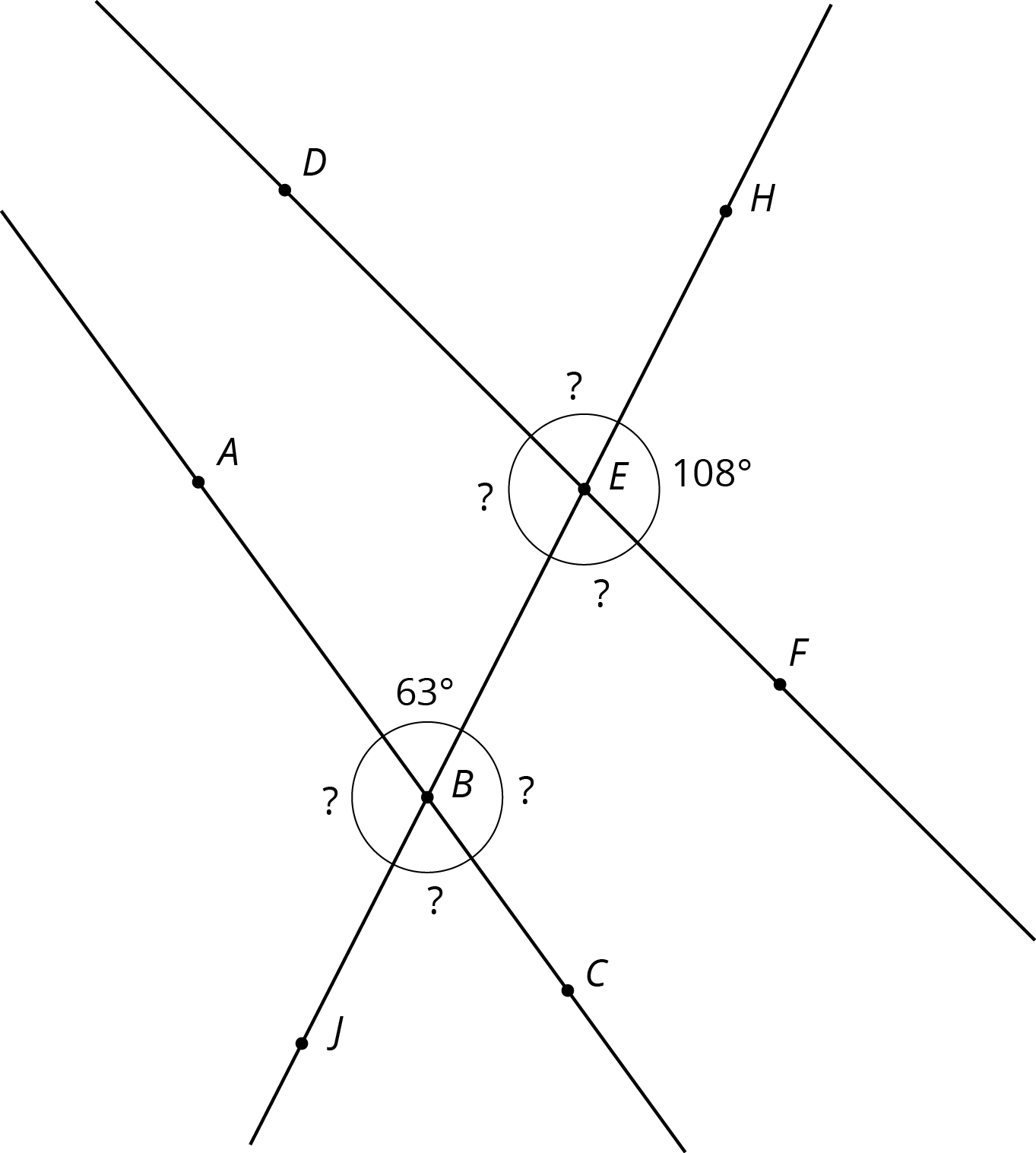
Lines and are parallel. They are cut by **transversal** .



1. With your partner, find the seven unknown angle measures in the diagram. Explain your reasoning.
2. What do you notice about the angles with vertex  and the angles with vertex ?
3. Using what you noticed, find the measures of the four angles at point in the second diagram. Lines and are parallel.

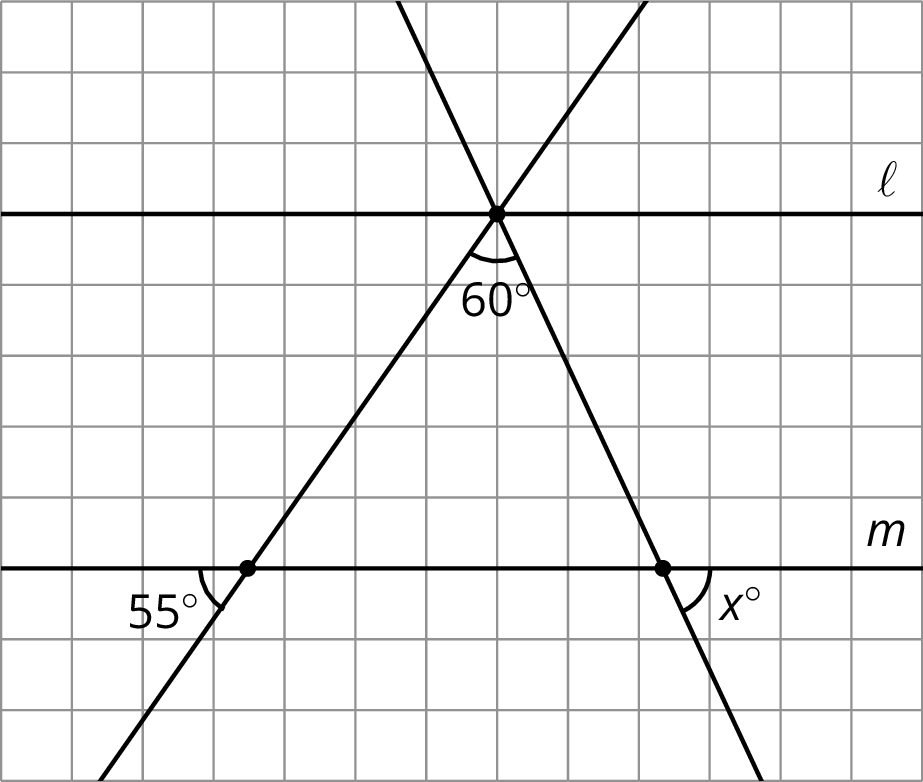
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1. The next diagram resembles the first one, but the lines form slightly different angles. Work with your partner to find the six unknown angles with vertices at points and .

* 

1. What do you notice about the angles in this diagram as compared to the earlier diagram? How are the two diagrams different? How are they the same?

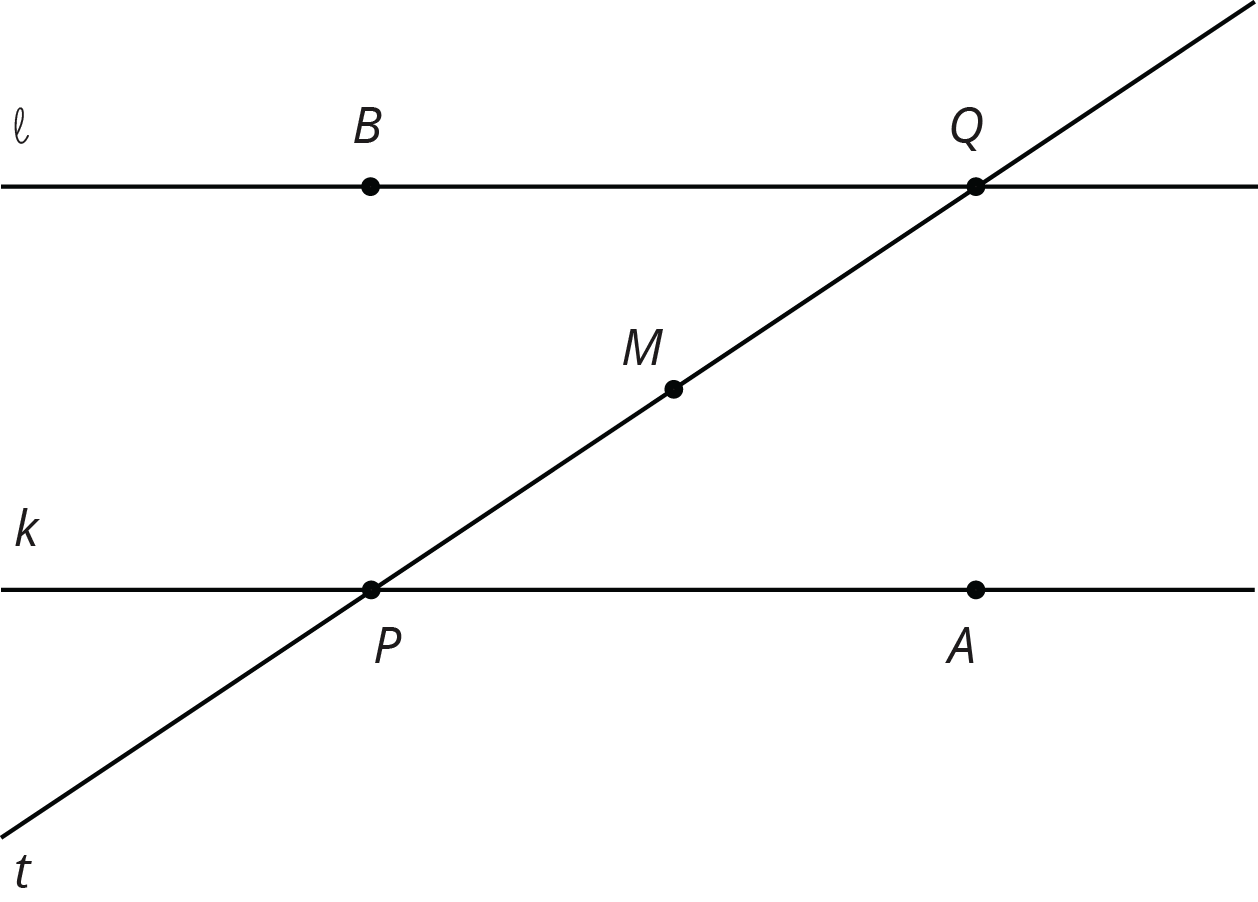
#### Are you ready for more?



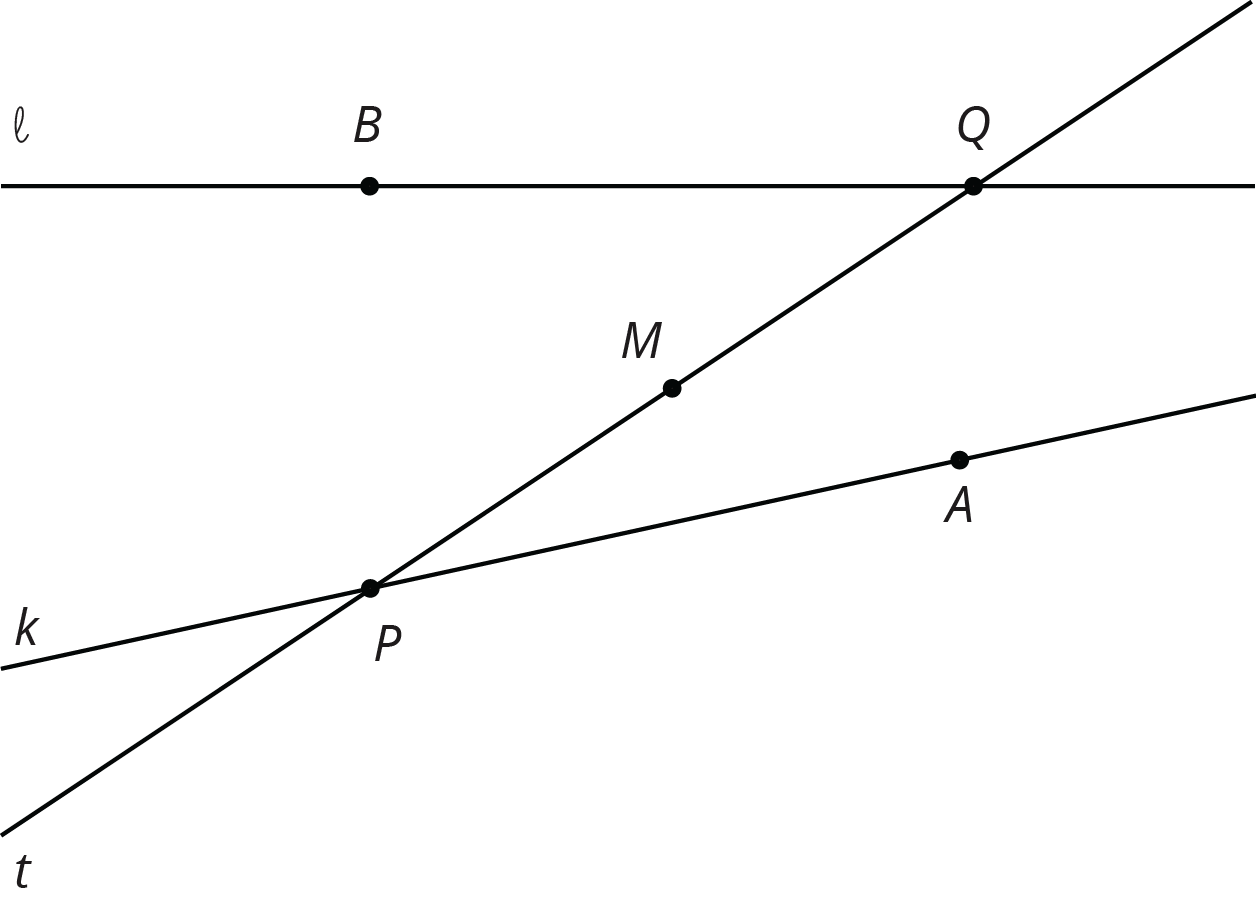
Parallel lines and are cut by two transversals which intersect in the same point. Two angles are marked in the figure. Find the measure of the third angle.

### 12.3: Alternate Interior Angles Are Congruent

1. Lines and are parallel and is a transversal. Point is the midpoint of segment .

* 
* Find a rigid transformation showing that angles and are congruent.

1. In this picture, lines and are no longer parallel. is still the midpoint of segment .

* 
* Does your argument in the earlier problem apply in this situation? Explain.

### 12.4: Info Gap: Angle Finding

Your teacher will give you either a *problem card* or a *data card*. Do not show or read your card to your partner.

If your teacher gives you the *problem card*:

1. Silently read your card and think about what information you need to be able to answer the question.
2. Ask your partner for the specific information that you need.
3. Explain how you are using the information to solve the problem.

* Continue to ask questions until you have enough information to solve the problem.

1. Share the *problem card* and solve the problem independently.
2. Read the *data card* and discuss your reasoning.

If your teacher gives you the *data card*:

1. Silently read your card.
2. Ask your partner *“What specific information do you need?”* and wait for them to *ask* for information.

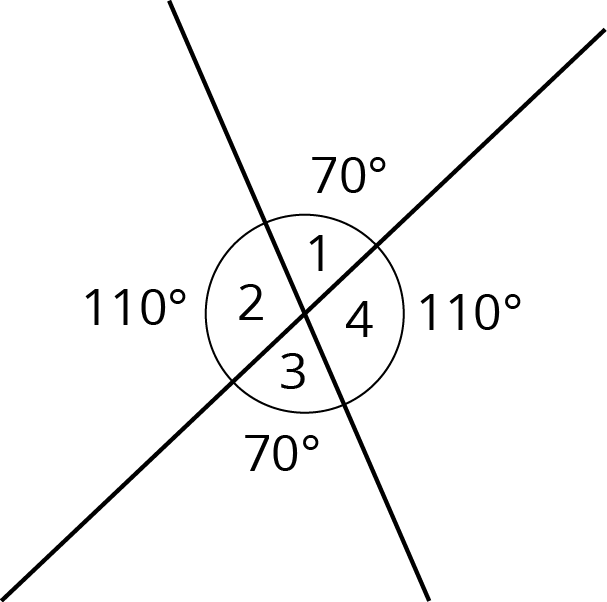
* If your partner asks for information that is not on the card, do not do the calculations for them. Tell them you don’t have that information.

1. Before sharing the information, ask “*Why do you need that information?*” Listen to your partner’s reasoning and ask clarifying questions.
2. Read the *problem card* and solve the problem independently.
3. Share the *data card* and discuss your reasoning.

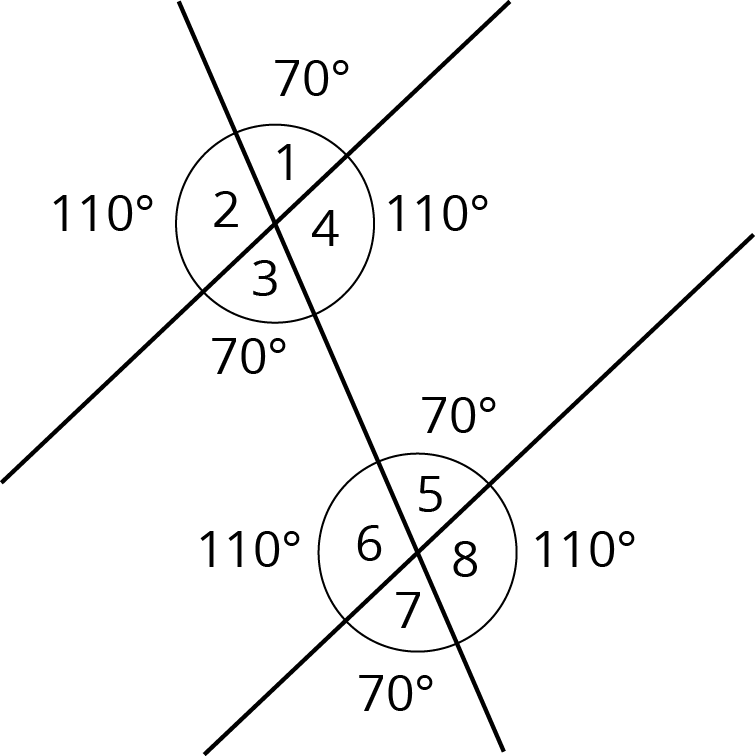
Pause here so your teacher can review your work. Ask your teacher for a new set of cards and repeat the activity, trading roles with your partner.

### Lesson 12 Summary

If two angle measures add up to , then we say the angles are **complementary**. If two angle measures add up to , then we say the angles are **supplementary**. When two lines intersect, vertical angles are equal and adjacent angles are supplementary. For example, in this figure angles 1 and 3 are equal, angles 2 and 4 are equal, angles 1 and 4 are supplementary, and angles 2 and 3 are supplementary.



When two parallel lines are cut by another line, called a **transversal**, two pairs of **alternate interior angles** are created. (“Interior” means on the inside, or between, the two parallel lines.) For example, in this figure angles 3 and 5 are alternate interior angles and angles 4 and 6 are also alternate interior angles.



Alternate interior angles are equal because a rotation around the midpoint of the segment that joins their vertices takes each angle to the other. Imagine a point halfway between the two intersections—can you see how rotating about takes angle 3 to angle 5?

Using what we know about vertical angles, adjacent angles, and alternate interior angles, we can find the measures of any of the eight angles created by a transversal if we know just one of them. For example, starting with the fact that angle 1 is we use vertical angles to see that angle 3 is , then we use alternate interior angles to see that angle 5 is , then we use the fact that angle 5 is supplementary to angle 8 to see that angle 8 is since . It turns out that there are only two different measures. In this example, angles 1, 3, 5, and 7 measure , and angles 2, 4, 6, and 8 measure .



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