

# **Lesson 13: Amplitude and Midline**

• Let's transform the graphs of trigonometric functions

# **13.1: Comparing Parabolas**

Match each equation to its graph.

Α

1. 
$$y = x^2$$

2. 
$$y = 3x^2$$

3. 
$$y = 3(x - 1)^2$$

4. 
$$y = 3x^2 - 1$$

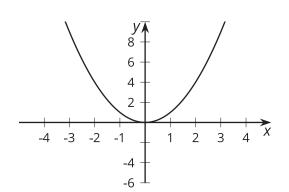
5. 
$$v = x^2 - 1$$

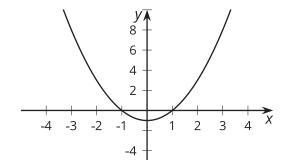
c

Ε

-4 -3 -2

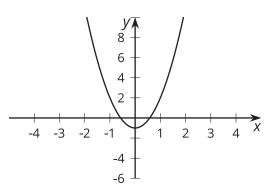


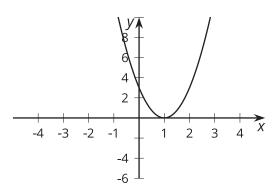




\_6 I

D

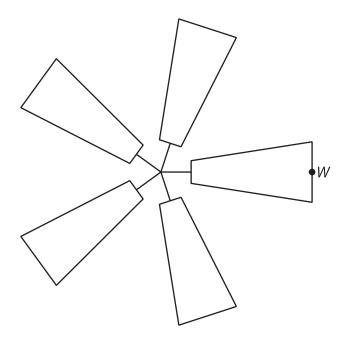




Be prepared to explain how you know which graph belongs with each equation.



## 13.2: Blowing in the Wind



Suppose a windmill has a radius of 1 meter and the center of the windmill is (0,0) on a coordinate grid.

- 1. Write a function describing the relationship between the height h of W and the angle of rotation  $\theta$ . Explain your reasoning.
- 2. Describe how your function and its graph would change if:
  - a. the windmill blade has length 3 meters.
  - b. The windmill blade has length 0.5 meter.
- 3. Test your predictions using graphing technology.

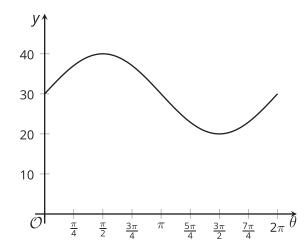


### 13.3: Up, Up, and Away

- 1. A windmill has radius 1 meter and its center is 8 meters off the ground. The point W starts at the tip of a blade in the position farthest to the right and rotates counterclockwise. Write a function describing the relationship between the height h of W, in meters, and the angle  $\theta$  of rotation.
- 2. Graph your function using technology. How does it compare to the graph where the center of windmill is at (0,0)?
- 3. What would the graph look like if the center of the windmill were 11 meters off the ground? Explain how you know.

### Are you ready for more?

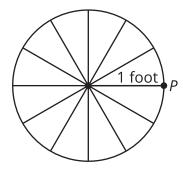
Here is the graph of a different function describing the relationship between the height y, in feet, of the tip of a blade and the angle of rotation  $\theta$  made by the blade. Describe the windmill.



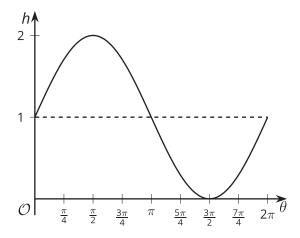


#### **Lesson 13 Summary**

Suppose a bike wheel has radius 1 foot and we want to determine the height of a point P on the wheel as it spins in a counterclockwise direction. The height h in feet of the point P can be modeled by the equation  $h = \sin(\theta) + 1$  where  $\theta$  is the angle of rotation of the wheel. As the wheel spins in a counterclockwise direction, the point first reaches a maximum height of 2 feet when it is at the top of the wheel, and then a minimum height of 0 feet when it is at the bottom.



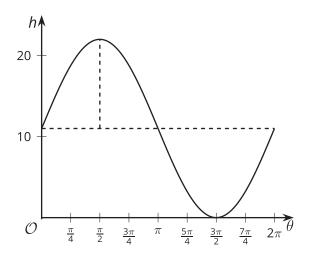
The graph of the height of P looks just like the graph of the sine function but it has been raised by 1 unit:



The horizontal line h = 1, shown here as a dashed line, is called the **midline** of the graph.

What if the wheel had a radius of 11 inches instead? How would that affect the height h, in inches, of point P over time? This wheel can also be modeled by a sine function,  $h=11\sin(\theta)+11$ , where  $\theta$  is the angle of rotation of the wheel. The graph of this function has the same wavelike shape as the sine function but its midline is at h=11 and its **amplitude** is different:





The amplitude of the function is the length from the midline to the maximum value, shown here with a dashed line, or, since they are the same, the length from the minimum value to the midline. For the graph of , the midline value is 11 and the maximum is 22. This means the amplitude is 11 since 22-11=11.