



# Edge Lengths, Volumes, and Cube Roots

Let's explore the relationship between volume and edge lengths of cubes.

## 12.1 Ordering Squares and Cubes

Let  $a$ ,  $b$ ,  $c$ ,  $d$ ,  $e$ , and  $f$  be positive numbers.

Given these equations, arrange  $a$ ,  $b$ ,  $c$ ,  $d$ ,  $e$ , and  $f$  from least to greatest. Explain your reasoning.

- $a^2 = 9$
- $b^3 = 8$
- $c^2 = 10$
- $d^3 = 9$
- $e^2 = 8$
- $f^3 = 7$



## 12.2

## Card Sort: Rooted in the Number Line

Your teacher will give you a set of cards. Each card has a number line with a plotted point, an equation, or a square or **cube root** value.

For each card with a letter and square or cube root value, match it with the location on a number line where the value exists, and the equation that the value makes true. Record your matches and be prepared to explain your reasoning.

## 12.3

## Cube Root Values

The value of a cube root of a number lies between two integers. Which are those consecutive whole numbers for the following? Be prepared to explain your reasoning.

1.  $\sqrt[3]{5}$

2.  $\sqrt[3]{23}$

3.  $\sqrt[3]{81}$

4.  $\sqrt[3]{999}$



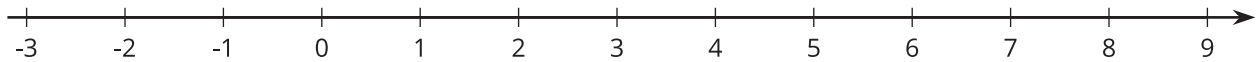
## 12.4 Solutions on a Number Line

The numbers  $x$ ,  $y$ , and  $z$  are positive, and:

$$x^3 = 5$$

$$y^3 = 27$$

$$z^3 = 700$$



1. Plot  $x$ ,  $y$ , and  $z$  on the number line. Be prepared to share your reasoning with the class.
2. Plot  $-\sqrt[3]{2}$  on the number line.

### Are you ready for more?

Diego knows that  $8^2 = 64$  and that  $4^3 = 64$ . He says that this means the following are all true:

- $\sqrt{64} = 8$
- $\sqrt[3]{64} = 4$
- $\sqrt{-64} = -8$
- $\sqrt[3]{-64} = -4$

Is he correct? Explain how you know.

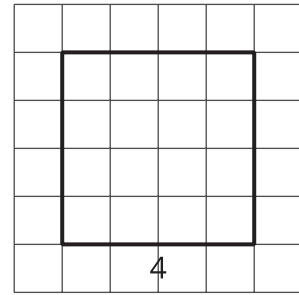
## Lesson 12 Summary

For a square, its side length is the square root of its area. For example, this square has an area of 16 square units and a side length of 4 units.

Both of these equations are true:

$$4^2 = 16$$

$$\sqrt{16} = 4$$

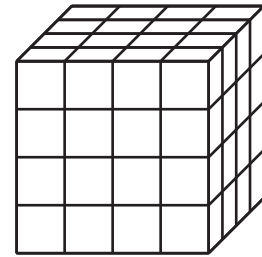


For a cube, the edge length is the **cube root** of its volume. For example, this cube has a volume of 64 cubic units and an edge length of 4 units:

Both of these equations are true:

$$4^3 = 64$$

$$\sqrt[3]{64} = 4$$



$\sqrt[3]{64}$  is pronounced “the cube root of 64.”

Like square roots, most cube roots of whole numbers are irrational. The only time the cube root of a number is a rational number is when the number we are taking the cube root of is a perfect cube. For example, 8 is a perfect cube, and  $\sqrt[3]{8} = 2$ .

We can approximate the values of the cube root of a number by observing the integers around it and remembering the relationship between cubes and cube roots. For example,  $\sqrt[3]{20}$  is between 2 and 3 since  $2^3 = 8$  and  $3^3 = 27$ , and 20 is between 8 and 27. Similarly, since 100 is between  $4^3$  and  $5^3$ , we know  $\sqrt[3]{100}$  is between 4 and 5.