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Using Factors and Zeros

Let's write some polynomials.

7.1

More Than Factors

M and K are both polynomial functions of x, where M(x) = (x+3)(2x-5) and K(x) = 3(x+3)(2x-5).

1. How are the two functions alike? How are they different?

2. If a graphing window of $-5 \le x \le 5$ and $-20 \le y \le 20$ shows all intercepts of a graph of y = M(x), what graphing window would show all intercepts of y = K(x)?

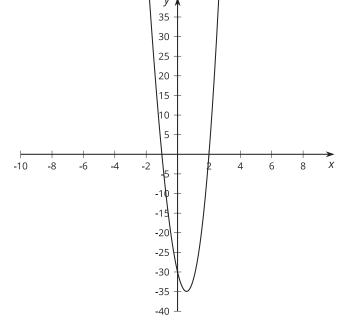


7.2

Choosing Windows

Mai graphs the function p given by p(x) = (x+1)(x-2)(x+15) and sees this graph.

She says, "This graph looks like a parabola, so it must be a quadratic."



- 1. Is Mai correct? Use graphing technology to check.
- 2. Explain how you could select a viewing window before graphing an expression like p(x) that would show the main features of a graph.

3. Using your explanation, what viewing window would you choose for graphing f(x) = (x+1)(x-1)(x-2)(x-28)?

Are you ready for more?

Select some different windows for graphing the function q(x) = 23(x - 53)(x - 18)(x + 111). What is challenging about graphing this function?

7.3

What's the Equation?

Write a possible equation for a polynomial whose graph has the following horizontal intercepts. Check your equation using graphing technology.

- 1. (4,0)
- 2. (0,0) and (4,0)
- 3. (-2,0), (0,0) and (4,0)
- 4. (-4,0), (0,0), and (2,0)
- 5. (-5,0), $(\frac{1}{2},0)$, and (3,0)

Lesson 7 Summary

We can use the zeros of a polynomial function to figure out what an expression for the polynomial might be. One way to write a polynomial expression is as a product of linear factors.

For example, for a polynomial function Z that satisfies Z(x) = 0 when x is -1, 2, or 4, we could multiply together a factor that is 0 when x = -1, a factor that is 0 when x = 2, and a factor that is 0 when x = 4. It turns out that there are many possible expressions for Z(x).

Using linear factors, one possibility is Z(x) = (x + 1)(x - 2)(x - 4).

Another possibility is Z(x) = 2(x+1)(x-2)(x-4), since the 2 (or any other rational number) does not change what values of x make the function equal to 0.

We can test the three values -1, 2, and 4 to make sure that Z(x) is 0 for those values. We can also graph both possible versions of Z and see that the graphs intercept the horizontal axis at -1, 2, and 4. Notice that while both functions have the same output at these three specific input values, they have different outputs for all other input values.

