# Reasoning about Exponential Graphs (Part 2)

Let's investigate what we can learn from graphs that represent exponential functions.

## 13.1

#### **Which Three Go Together: Four Functions**

Which three go together? Why do they go together?

$$A(n) = 8 \cdot 3^n$$

$$B(n) = 2 \cdot 8^n$$

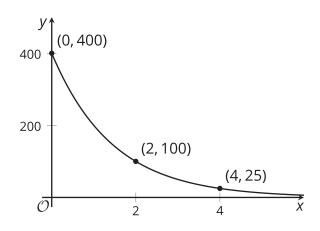
$$C(n) = 8 + 2n$$

$$D(n) = 8 \cdot \left(\frac{1}{2}\right)^n$$

### 13.2

### **Value of a Computer**

1. Here is a graph representing an exponential function, f. The function, f, gives the value of a computer, in dollars, as a function of time, x, measured in years since the time of purchase.



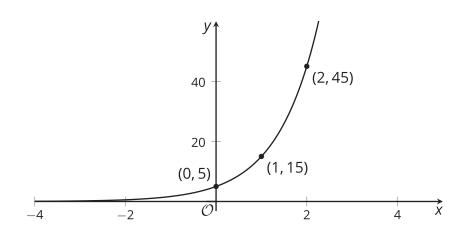
Based on the graph, what can you say about the following?

- a. The purchase price of the computer
- b. The value of f when x is 1
- c. The meaning of f(1)

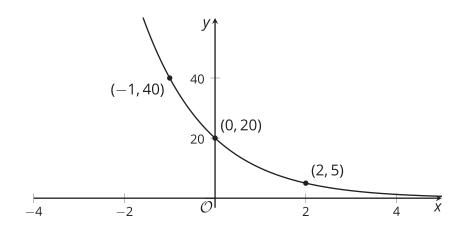


- d. How the value of the computer is changing each year
- e. An equation that defines f
- f. Whether the value of f will reach 0 after 10 years
- 2. Here are graphs of two exponential functions. For each, write an equation that defines the function, and find the value of the function when x is 5.

a.



b.





#### Are you ready for more?

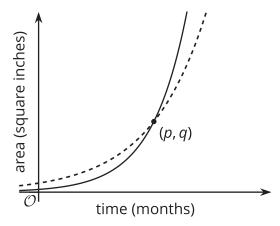
Consider a function f defined by  $f(x) = a \cdot b^x$ .

- If the graph of f goes through the points (2, 10) and (8, 30), would you expect f(5) to be less than, equal to, or greater than 20?
- If the graph of f goes through the points (2,30) and (8,10), would you expect f(5) to be less than, equal to, or greater than 20?

# 13.3

#### **Moldy Wall**

Here are graphs representing two functions, and descriptions of two functions.



- Function *f*: The area of a wall that is covered by Mold A, in square inches, doubling every month.
- Function *g*: The area of a wall that is covered by Mold B, in square inches, tripling every month.
- 1. Which graph represents each function? Label the graphs accordingly and explain your reasoning.
- 2. When the mold was first spotted and measured, was there more of Mold A or Mold B? Explain how you know.
- 3. What does the point (p, q) tell us in this situation?



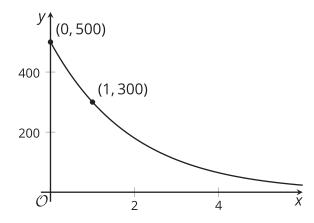
#### Lesson 13 Summary

If we have enough information about a graph representing an exponential function f, we can write a corresponding equation.

Here is a graph of y = f(x).

An equation defining an exponential function has the form  $f(x) = a \cdot b^x$ . The value of a is the starting value or f(0), so it is the y-intercept of the graph. We can see that f(0) is 500 and that the function is decreasing.

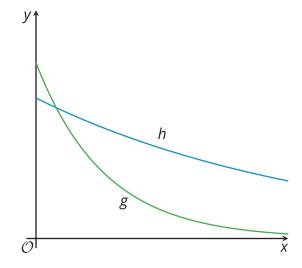
The value of b is the growth factor. It is the number by which we multiply the function's output at x to get the output at x+1. To find this growth factor for f, we can calculate  $\frac{f(1)}{f(0)}$ , which is  $\frac{300}{500}$  (or  $\frac{3}{5}$ ).



So an equation that defines f is:  $f(x) = 500 \cdot \left(\frac{3}{5}\right)^x$ 

We can also use graphs to compare functions. Here are graphs representing two different exponential functions, labeled g and h. Each one represents the area of algae (in square meters) in a pond, x days after certain fish were introduced.

- Pond A had 40 square meters of algae. Its area shrinks to  $\frac{8}{10}$  of the area on the previous day.
- Pond B had 50 square meters of algae. Its area shrinks to  $\frac{2}{5}$  of the area on the previous day.



Can you tell which graph corresponds to which algae population?

We can see that the y-intercept of g's graph is greater than the y-intercept of h's graph. We can also see that g has a smaller growth factor than h because as x increases by the same amount, g is retaining a smaller fraction of its value compared to h. This suggests that g corresponds to Pond B, and h corresponds to Pond A.

