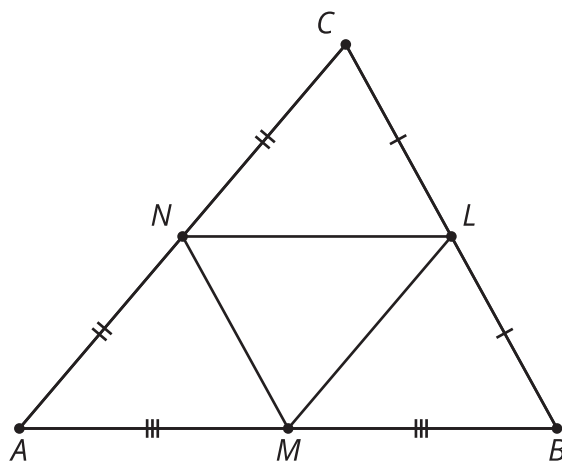


Lesson 5: Splitting Triangle Sides with Dilation, Part 1

- Let's draw segments connecting midpoints of the sides of triangles.

5.1: Notice and Wonder: Midpoints

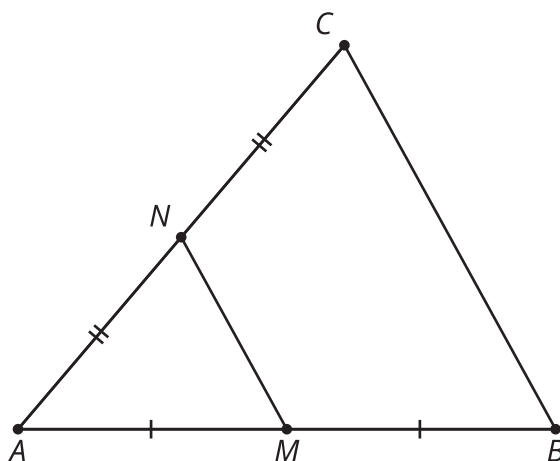
Here's a triangle ABC with midpoints L , M , and N .



What do you notice? What do you wonder?

5.2: Dilation or Violation?

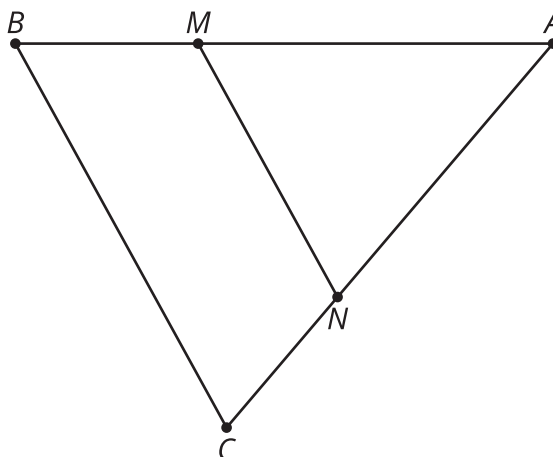
Here's a triangle ABC . Points M and N are the midpoints of 2 sides.



1. Convince yourself triangle ABC is a dilation of triangle AMN . What is the center of the dilation? What is the scale factor?
2. Convince your partner that triangle ABC is a dilation of triangle AMN , with the center and scale factor you found.
3. With your partner, check the definition of dilation on your reference chart and make sure both of you could convince a skeptic that ABC definitely fits the definition of dilation.
4. Convince your partner that segment BC is twice as long as segment MN .
5. Prove that $BC = 2MN$. Convince a skeptic.

5.3: A Little Bit Farther Now

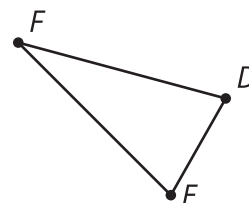
Here's a triangle ABC . M is $\frac{2}{3}$ of the way from A to B . N is $\frac{2}{3}$ of the way from A to C .



What can you say about segment MN , compared to segment BC ? Provide a reason for each of your conjectures.

Are you ready for more?

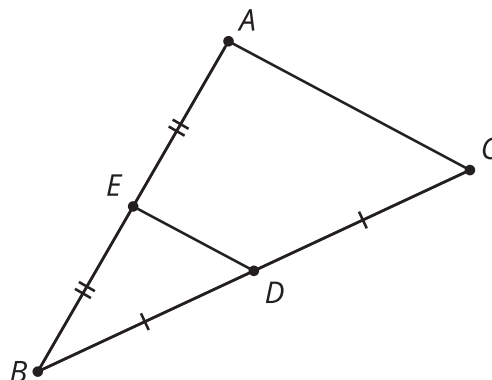
1. Dilate triangle DEF using a scale factor of -1 and center F .
2. How does DF compare to $D'F'$?
3. Are E , F , and E' collinear? Explain or show your reasoning.



Lesson 5 Summary

Let's examine a segment whose endpoints are the midpoints of 2 sides of the triangle. If D is the midpoint of segment BC and E is the midpoint of segment BA , then what can we say about ED and triangle ABC ?

Segment ED is parallel to the third side of the triangle and half the length of the third side of the triangle. For example, if $AC = 10$, then $ED = 5$. This happens because the entire triangle EBD is a dilation of triangle ABC with a scale factor of $\frac{1}{2}$.



In triangle ABC , segment FG divides segments AB and CB proportionally. In other words, $\frac{BG}{GA} = \frac{BF}{FC}$. Again, there is a dilation that takes triangle ABC to triangle GBF , so FG is parallel to AC and we can calculate its length using the same scale factor.

$$\overrightarrow{FG} \parallel \overrightarrow{AC}$$

