



Finding and Interpreting the Mean as the Balance Point

Let's look at another way to understand the mean of a data set.

10.1 Which Three Go Together: Division

Which three go together? Why do they go together?

A

$$\frac{5 + 5 + 5 + 5}{4}$$

B

$$\frac{10 + 6 + 4}{4}$$

C

$$\frac{10 + 8 + 6 + 4}{4}$$

D

$$\frac{7 + 6 + 4 + 2 + 1}{5}$$

10.2 Travel Times (Part 1)

Here are data showing how long it takes for Diego to walk to school, in minutes, over 5 days. The mean number of minutes is 11.

12 7 13 9 14

1. Represent Diego's data on a dot plot. Mark the location of the mean with a triangle.



2. The mean can also be seen as a **measure of center** that balances the points in a data set. If we find the distance between every point and the mean, add the distances on each side of the mean, and compare the two sums, we can see this balancing.

- a. Record the distance between each point and 11 and its location relative to 11.

time in minutes	distance from 11	left of 11 or right of 11?
12	1	right
7	4	left
13		
9		
14		

- b. Sum of distances left of 11:_____ Sum of distances right of 11:_____

What do you notice about the two sums?

3. Can another point that is not the mean produce similar sums of distances?

Let's investigate whether 10 can produce similar sums as those of 11.

- a. Complete the table with the distance of each data point from 10.

time in minutes	distance from 10	left of 10 or right of 10?
12		
7		
13		
9		
14		

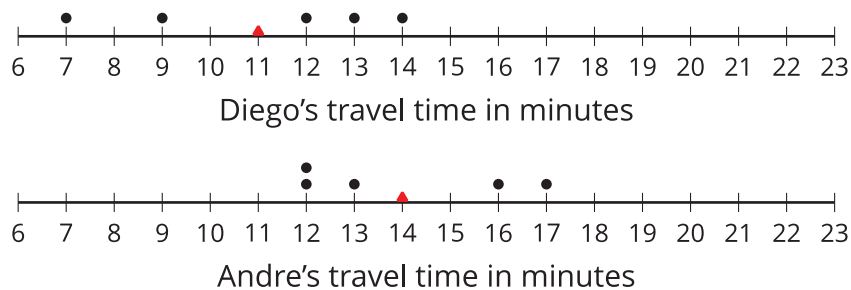
- b. Sum of distances left of 10:_____ Sum of distances right of 10:_____

What do you notice about the two sums?

4. Based on your work so far, explain why the mean can be considered a balance point for the data set.

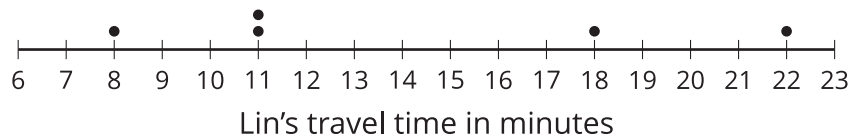
10.3 Travel Times (Part 2)

1. Here are dot plots showing how long Diego's trips to school took in minutes and how long Andre's trips to school took in minutes. The dot plots include the means for each data set, and those means are marked by triangles.



- a. Which of the two data sets has a larger mean? In this context, what does a larger mean tell us?
- b. Which of the two data sets has larger sums of distances to the left and right of the mean? What do these sums tell us about the variability in Diego's and Andre's travel times?

2. Here is a dot plot showing lengths of Lin's trips to school.



- a. Calculate the mean of Lin's travel times.
- b. Complete the table with the distance between each point and the mean as well whether the point is to the left or right of the mean.

time in minutes	distance from the mean	left or right of the mean?
22		
18		
11		
8		
11		

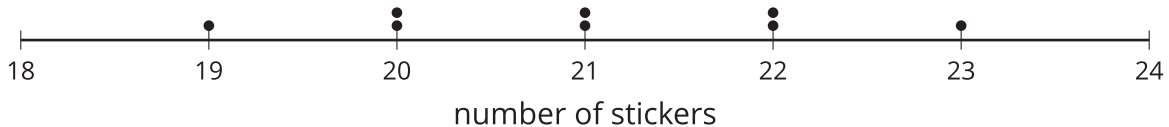
- c. Find the sum of distances to the left of the mean and the sum of distances to the right of the mean.
- d. Use your work to compare Lin's travel times to Andre's. What can you say about their average travel times? What about the variability in their travel times?

Lesson 10 Summary

The mean is often used as a **measure of center** of a distribution. One way to see this is that the mean of a distribution can be seen as the “balance point” for the distribution. Why is this a good way to think about the mean? Let’s look at a very simple set of data on the number of stickers that are on 8 pages:

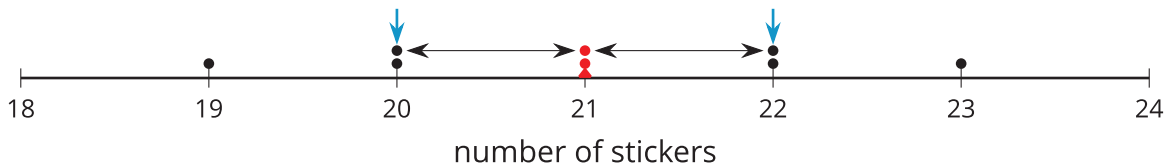
19 20 20 21 21 22 22 23

Here is a dot plot showing the data set.

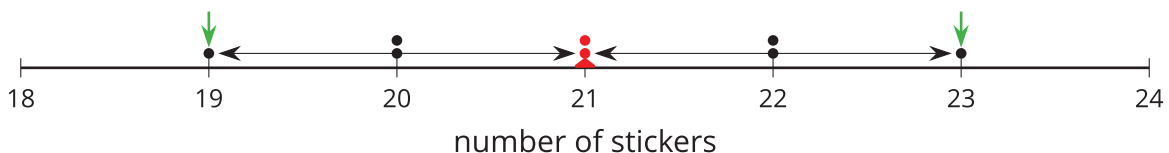


The distribution shown is completely symmetrical. The mean number of stickers is 21, because $(19 + 20 + 20 + 21 + 21 + 22 + 22 + 23) \div 8 = 21$. If we mark the location of the mean on the dot plot, we can see that the data points could balance at 21.

In this plot, each point on either side of the mean has a mirror image. For example, the two points at 20 and the two at 22 are the same distance from 21, but each pair is located on either side of 21. We can think of them as balancing each other around 21.



Similarly, the points at 19 and 23 are the same distance from 21 but are on either side of it. They, too, can be seen as balancing each other around 21.



We can say that the distribution of the stickers has a center at 21 because that is its balance point, and that the eight pages, on average, have 21 stickers.

Even when a distribution is not completely symmetrical, the distances of values below the mean, on the whole, balance the distances of values above the mean.