



Part to Whole

Let's see what we can figure out about a circle if we're given information about a sector of the circle.

9.1 What's Your Angle?

A circle has radius 10 centimeters. Suppose an arc on the circle has length π centimeters. What is the measure of the central angle whose radii define the arc?

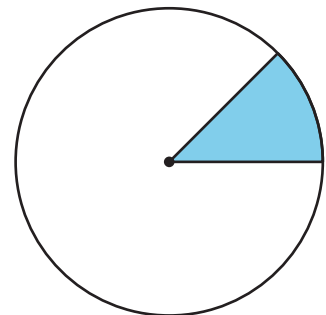
9.2 Enough Information?

The central angle of this shaded sector measures 45 degrees, and the sector's area is 32π square inches.

Kiran says, "We can find the area of the whole circle, the arc length of the sector, and the circumference of the circle with this information."

Priya says, "But how? We don't know the circle's radius!"

Do you agree with either of them? Explain or show your reasoning. Calculate as many of the values Kiran mentioned as possible.

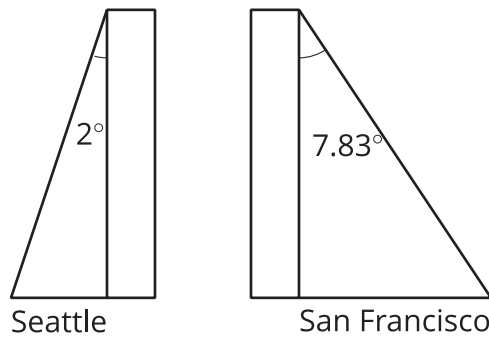


 Are you ready for more?

A Greek mathematician named Eratosthenes (eh-ruh-TAAS-thuh-nee-z) calculated the circumference of Earth more than 2,000 years ago. He used information similar to what is given here:

Seattle and San Francisco are on the same longitude line and 680 miles apart. At noon on a summer day, an upright meter stick in Seattle casts a shadow with an angle of 2 degrees. On the same day at the same time, an upright meter stick in San Francisco casts a shadow with an angle of 7.83 degrees.

image not to scale



Use this information to calculate the circumference of Earth. Explain or show your reasoning.

9.3

Info Gap: From Sector to Circle

Your teacher will give you either a problem card or a data card. Do not show or read your card to your partner.

If your teacher gives you the problem card:

1. Silently read your card and think about what information you need to answer the question.
2. Ask your partner for the specific information that you need. "Can you tell me _____?"
3. Explain to your partner how you are using the information to solve the problem. "I need to know _____ because _____." Continue to ask questions until you have enough information to solve the problem.
4. Once you have enough information, share the problem card with your partner, and solve the problem independently.
5. Read the data card, and discuss your reasoning.

If your teacher gives you the data card:

1. Silently read your card. Wait for your partner to ask for information.
2. Before telling your partner any information, ask, "Why do you need to know _____?"
3. Listen to your partner's reasoning and ask clarifying questions. Only give information that is on your card. Do not figure out anything for your partner! These steps may be repeated.
4. Once your partner says they have enough information to solve the problem, read the problem card, and solve the problem independently.
5. Share the data card, and discuss your reasoning.

Lesson 9 Summary

We can work backward from information about a sector or arc to get information about the whole circle.

Suppose a circle has an arc with length 7π units that is defined by a 90-degree central angle. This arc makes up $\frac{1}{4}$ the entire circumference of the circle because $360 \div 90 = 4$. So we can multiply the arc's length by 4 to find that the entire circumference measures 28π units. The circumference of a circle can be calculated using the expression $2\pi r$, so we know that $2\pi r = 28\pi$. The value of r must be 14 units.

For more difficult problems, we can write equations. Suppose a circle has a sector with area 135π square units and a central angle of 216 degrees. Let x stand for the area of the whole circle. Dividing 216 by 360 gives the fraction of the circle represented by the sector. Multiply that fraction by x and set it equal to the area of the sector.

$$\frac{216}{360}x = 135\pi$$

Solve this equation to find that the circle's area is 225π square units. This tells us that $\pi r^2 = 225\pi$. The value of r must be the positive number that squares to make 225, or 15 units.