

# **Lesson 2: Truth and Equations**

Let's use equations to represent stories and see what it means to solve equations.

### 2.1: Three Letters

- 1. The equation a + b = c could be true or false.
  - a. If *a* is 3, *b* is 4, and *c* is 5, is the equation true or false?
  - b. Find new values of a, b, and c that make the equation true.
  - c. Find new values of *a*, *b*, and *c* that make the equation false.
- 2. The equation  $x \cdot y = z$  could be true or false.
  - a. If *x* is 3, *y* is 4, and *z* is 12, is the equation true or false?
  - b. Find new values of x, y, and z that make the equation true.
  - c. Find new values of x, y, and z that make the equation false.



### 2.2: Storytime

Here are three situations and six equations. Which equation best represents each situation? If you get stuck, consider drawing a diagram.

$$x + 5 = 20$$

$$x = 20 + 5$$

$$5x = 20$$

$$x + 20 = 5$$

$$5 \cdot 20 = x$$

$$20x = 5$$

1. After Elena ran 5 miles on Friday, she had run a total of 20 miles for the week. She ran x miles before Friday.

2. Andre's school has 20 clubs, which is five times as many as his cousin's school. His cousin's school has x clubs.

3. Jada volunteers at the animal shelter. She divided 5 cups of cat food equally to feed 20 cats. Each cat received x cups of food.



## 2.3: Using Structure to Find Solutions

Here are some equations that contain a **variable** and a list of values. Think about what each equation means and find a **solution** in the list of values. If you get stuck, consider drawing a diagram. Be prepared to explain why your solution is correct.

1. 
$$1000 - a = 400$$

$$2.12.6 = b + 4.1$$

$$3.8c = 8$$

4. 
$$\frac{2}{3} \cdot d = \frac{10}{9}$$

$$5.10e = 1$$

6. 
$$10 = 0.5 f$$

$$7.0.99 = 1 - g$$

8. 
$$h + \frac{3}{7} = 1$$

List: 
$$\frac{1}{8}$$
  $\frac{3}{7}$   $\frac{4}{7}$   $\frac{3}{5}$   $\frac{5}{3}$   $\frac{7}{3}$  0.01 0.1 0.5



#### Are you ready for more?

One solution to the equation a + b + c = 10 is a = 2, b = 5, c = 3.

How many different whole-number solutions are there to the equation a+b+c=10? Explain or show your reasoning.

#### **Lesson 2 Summary**

An equation can be true or false. An example of a true equation is  $7 + 1 = 4 \cdot 2$ . An example of a false equation is 7 + 1 = 9.

An equation can have a letter in it, for example, u + 1 = 8. This equation is false if u is 3, because 3 + 1 does not equal 8. This equation is true if u is 7, because 7 + 1 = 8.

A letter in an equation is called a **variable**. In u + 1 = 8, the variable is u. A number that can be used in place of the variable that makes the equation true is called a **solution** to the equation. In u + 1 = 8, the solution is 7.

When a number is written next to a variable, the number and the variable are being multiplied. For example, 7x = 21 means the same thing as  $7 \cdot x = 21$ . A number written next to a variable is called a **coefficient**. If no coefficient is written, the coefficient is 1. For example, in the equation p + 3 = 5, the coefficient of p is 1.