Algebra 1  
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Unit 6, Lesson 5

# Understanding Decay

Let’s look at exponential decay.

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## 5.1Notice and Wonder: Two Tables

What do you notice? What do you wonder?

Table A

|  |  |
| --- | --- |
| 0 | 2 |
| 1 |  |
| 2 | 5 |
| 3 |  |
| 4 | 8 |

Table B

|  |  |
| --- | --- |
| 0 | 2 |
| 1 | 3 |
| 2 |  |
| 3 |  |
| 4 |  |

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## 5.2What's Left?

1. Here is one way to think about how much Diego has left after spending of $100. Explain each step.
   * Step 1:
   * Step 2:
   * Step 3:
   * Step 4:
2. A person makes $1,800 per month, but of that amount goes to her rent. What two numbers can you multiply to find out how much she has after paying her rent?
3. Write an expression that uses only multiplication and that is equivalent to reduced by of .

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## 5.3Value of a Vehicle

Every year after a new car is purchased, it loses of its value. Let’s say that a new car costs $18,000.

1. A buyer worries that the car will be worth nothing in three years. Do you agree? Explain your reasoning.
2. If the car loses of its value every year, how much is the car still worth?

* Pause here for a whole-group discussion.

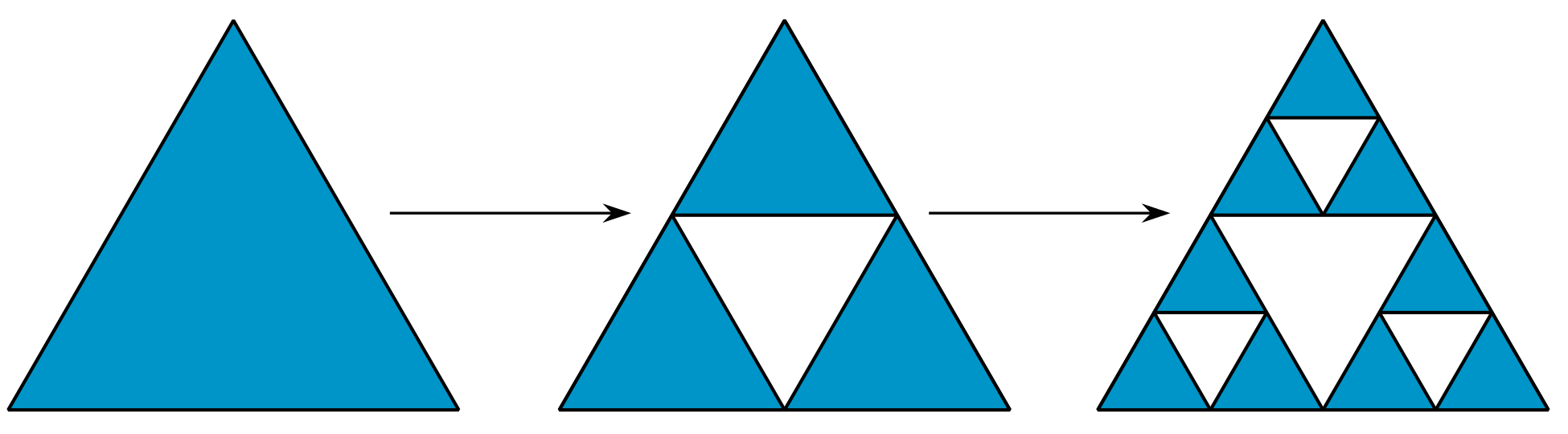
1. Write an expression to show how to find the value of the car for each year listed in the table.

|  |  |
| --- | --- |
| * year | * value of car (dollars) |
| * 0 | * 18,000 |
| * 1 |  |
| * 2 |  |
| * 3 |  |
| * 6 |  |
|  |  |

1. Write an equation relating the value of the car in dollars, , to the number of years, .
2. Use your equation to find when is 0. What does this value of mean in this situation?
3. A different car loses value at a different rate. The value of this different car in dollars, , after years can be represented by the equation . Explain what the numbers 10,000 and mean in this situation.

### Are you ready for more?

Start with an equilateral triangle with area 1 square unit, divide it into 4 congruent pieces as in the figure, and remove the middle one. Then, repeat this process with each of the remaining pieces. Repeat this process over and over for the remaining pieces. The figure shows the first two steps of this construction.



What fraction of the area is removed each time? How much area remains after the -th step? Use a calculator to find out how much area *remains* in the triangle after 50 such steps have been taken.

## Lesson 5 Summary

Sometimes a quantity grows by the same factor at regular intervals. For example, a population might double every year. Sometimes a quantity *decreases*by the same factor at regular intervals. For example, a car might lose one third of its value every year.

Let's look at a situation in which the quantity decreases by the same factor at regular intervals. Suppose a bacteria population starts at 100,000, and of the population dies each day. The population one day later is , which can be written as . The population after one day is of 100,000 or 75,000. The population after two days is . Here are some further values for the bacteria population

| number of days | bacteria population |
| --- | --- |
| 0 | 100,000 |
| 1 | 75,000 (or ) |
| 2 | 56,250 (or , or ) |
| 3 | about 42,188 (or , or ) |

In general, days after the bacteria population was 100,000, the population  is given by the equation: with one factor of for each day.

Situations with quantities that decrease exponentially are described with the term *exponential decay.* The multiplier ( in this case) is still called the *growth factor*, though sometimes people call it the *decay factor* instead.