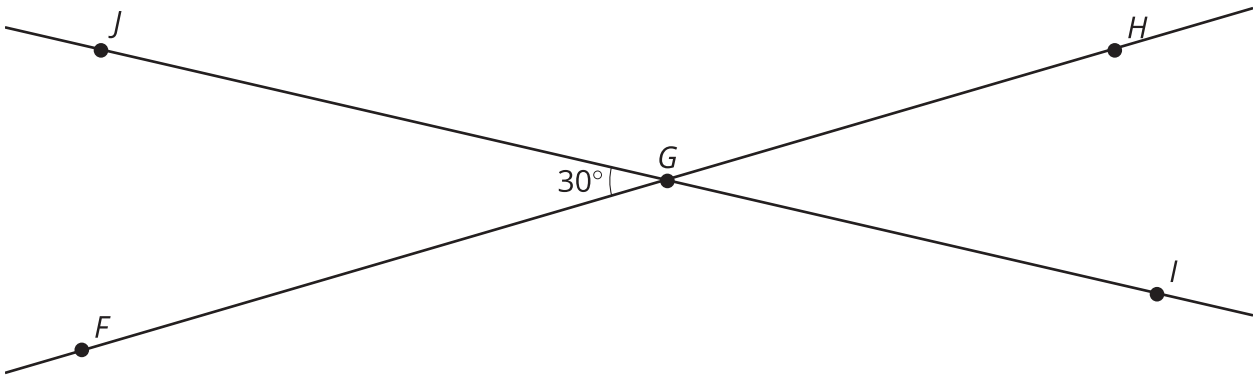
Unit 1, Lesson 14

Alternate Interior Angles

Let's explore why some angles are always equal.

14.1 Angle Pairs

1. Find the measure of angle JGH. Explain or show your reasoning.



2. Find and label a second 30° angle in the diagram. Find and label an angle congruent to angle JGH.

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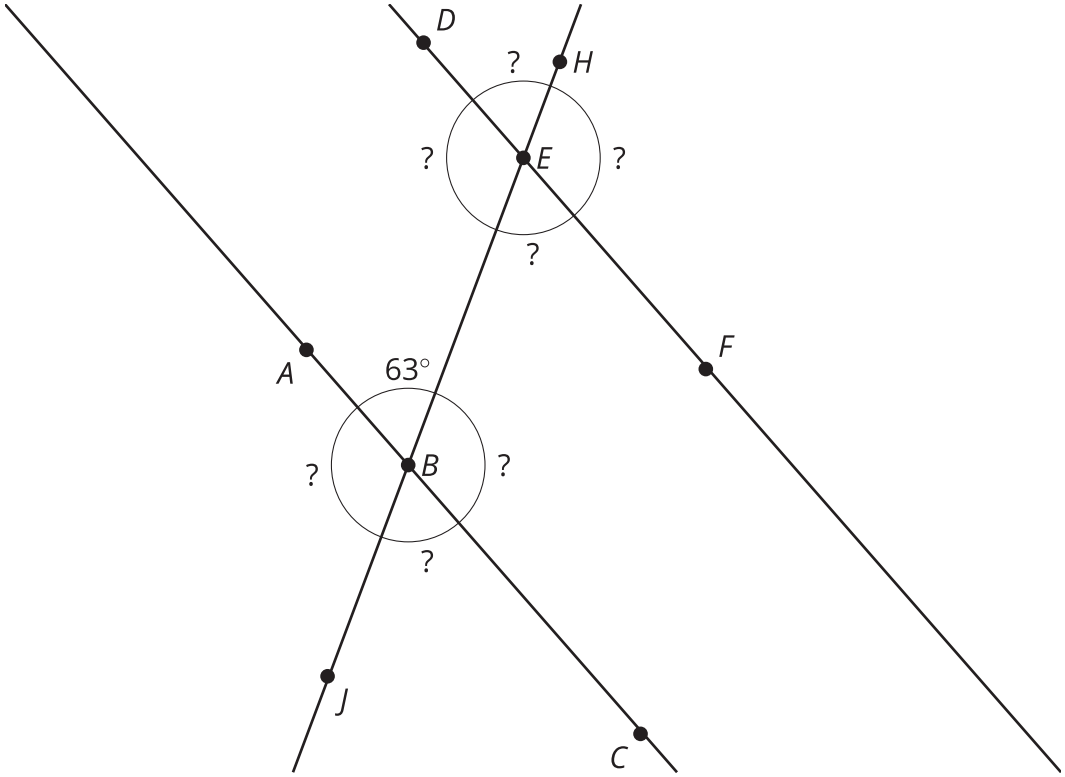
14.2 Cutting Parallel Lines with a Transversal

Lines AC and DF are parallel. They are cut by **transversal** HJ.



1. With your partner, find the seven unknown angle measures in the diagram. Explain your reasoning.

2. What do you notice about the angles with vertex B and the angles with vertex E?

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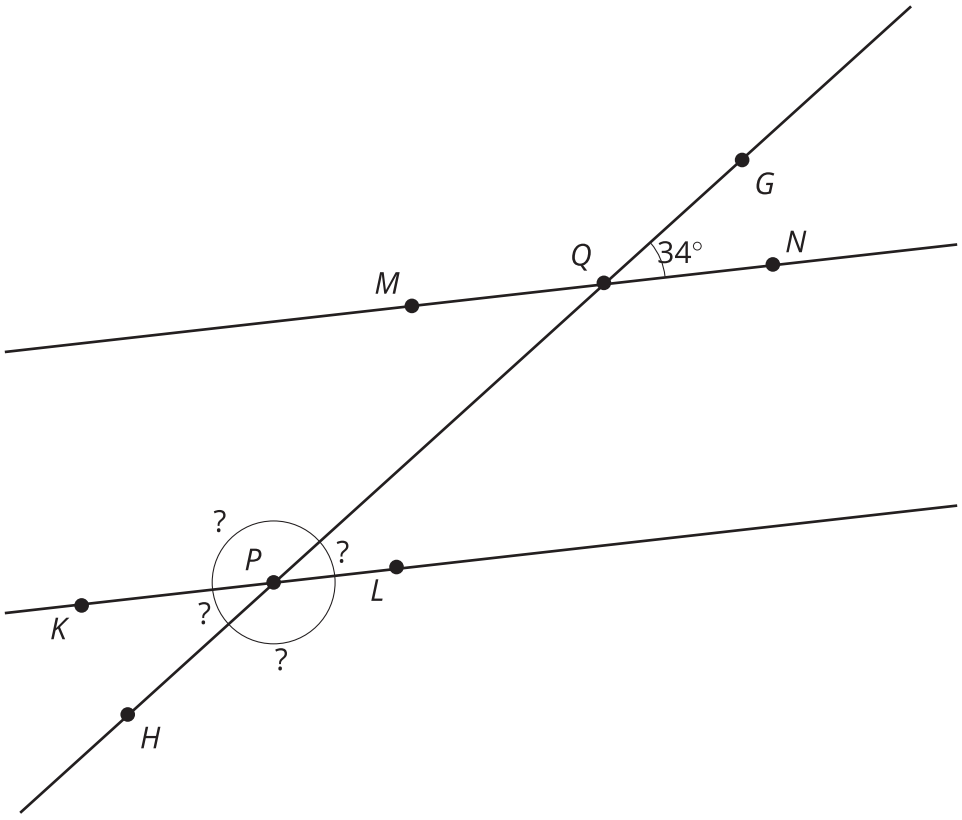
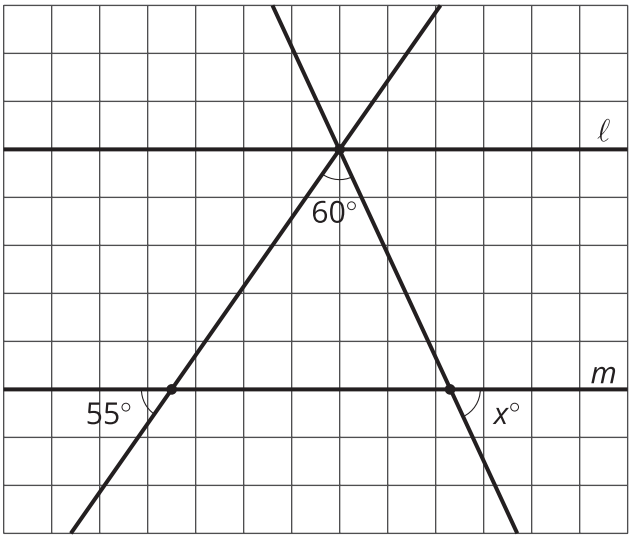
3. Using what you noticed, find the measures of the four angles at point P in the diagram. Lines KL and MN are parallel.



Are you ready for more?

Parallel lines ℓ and m are cut by two transversals that intersect ℓ at the same point. Two angles are marked in the figure. Find the measure x of the third angle.



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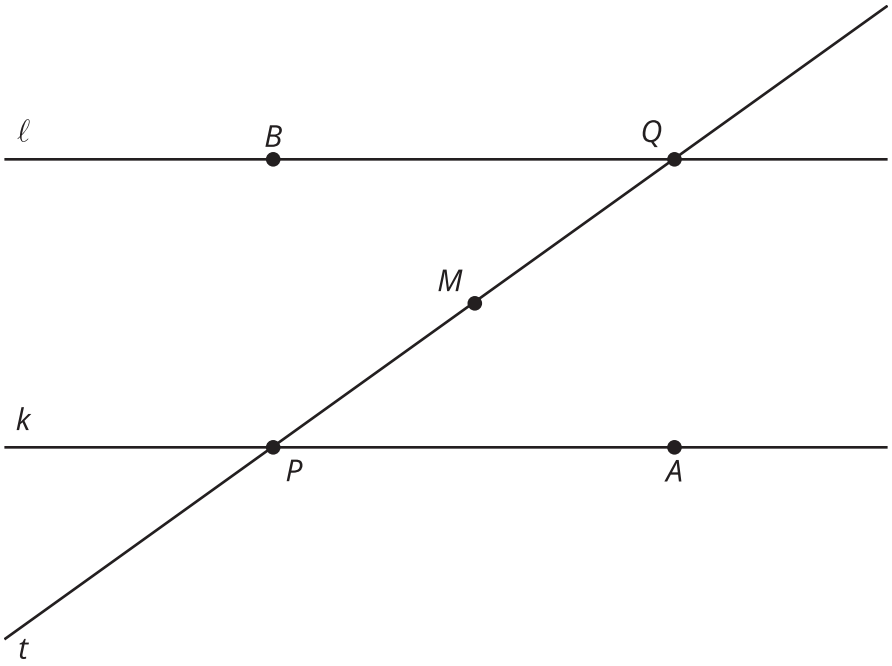
14.3 Alternate Interior Angles Are Congruent



Lines ℓ and k are parallel and t is a transversal. Point M is the midpoint of segment PQ.

Find a rigid transformation showing that angles MPA and MQB are congruent.

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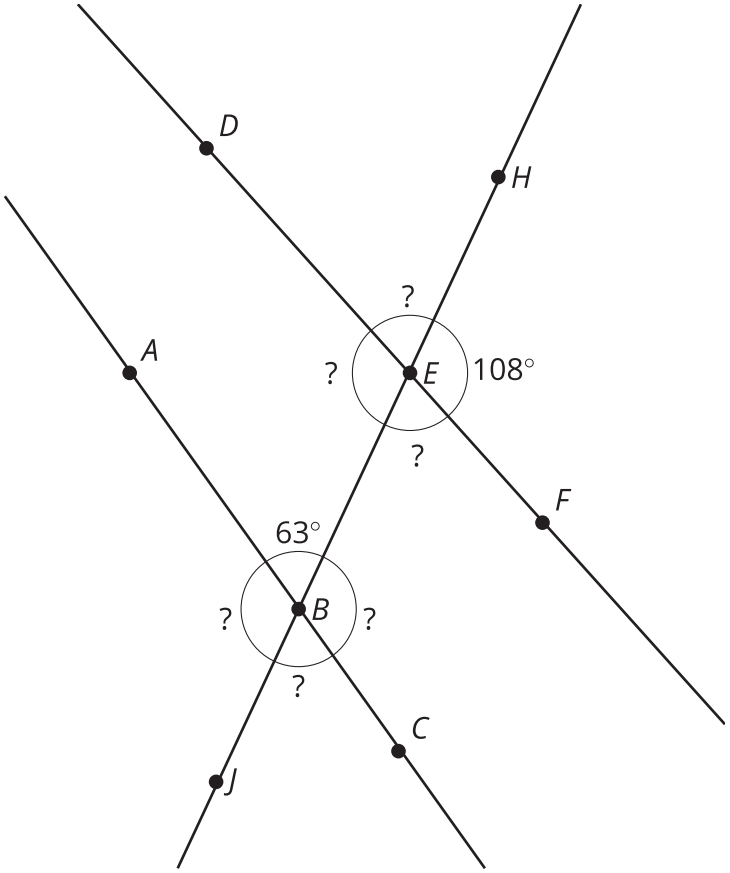
14.4 Not Parallel

1. Lines DF and AC are not parallel in this image.

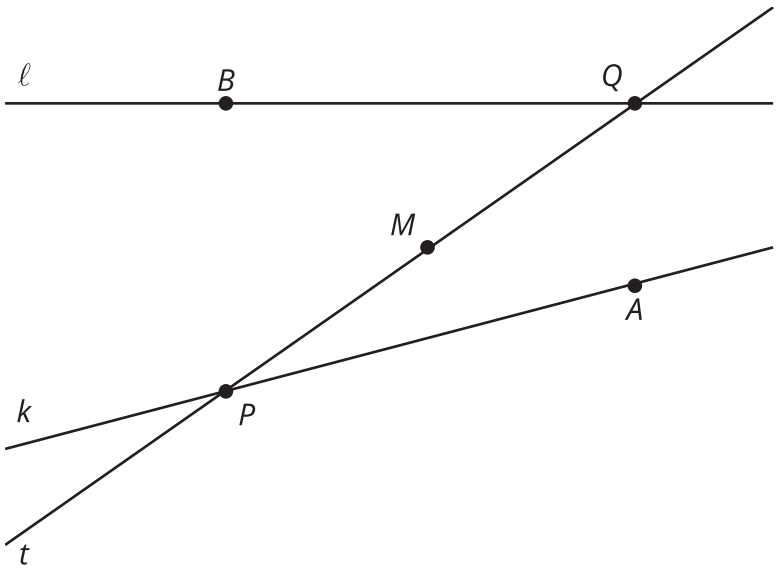


Find the missing angle measures around point E and point B.

What do you notice about the angles in this diagram?

2. Point M is the midpoint of line segment QP.

Can you find a rigid transformation that shows angle BQM is congruent to angle MPA? Explain your reasoning.



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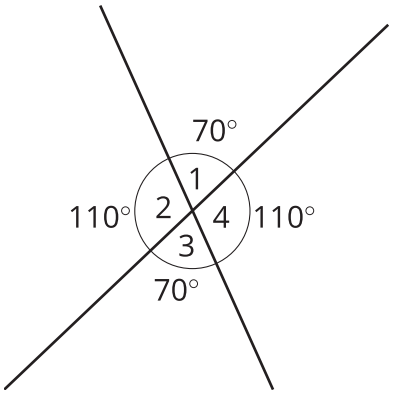
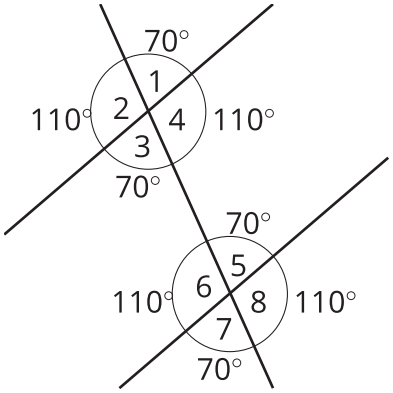
Lesson 14 Summary

When two lines intersect, vertical angles are congruent, and adjacent angles are supplementary, so their measures sum to 180. For example, in this figure angles 1 and 3 are congruent, angles 2 and 4 are congruent, angles 1 and 4 are supplementary, and angles 2 and 3 are supplementary.



When two parallel lines are cut by another line, called a **transversal**, two pairs of **alternate interior angles** are created. ("Interior" means on the inside, or between, the two parallel lines.) For example, in this figure angles 3 and 5 are alternate interior angles and angles 4 and 6 are also alternate interior angles.



Alternate interior angles are equal because a 180° rotation around the midpoint of the segment that joins their vertices takes each angle to the other. Imagine a point M halfway between the two intersections. Can you see how rotating 180° about M takes angle 3 to angle 5?

Using what we know about vertical angles, adjacent angles, and alternate interior angles, we can find the measures of any of the eight angles created by a transversal if we know just one of them. For example, starting with the fact that angle 1 is 70° we use vertical angles to see that angle 3 is 70°, then we use alternate interior angles to see that angle 5 is 70°, then we use the fact that angle 5 is supplementary to angle 8 to see that angle 8 is 110° since $180 - 70 = 110$. It turns out that there are only two different measures. In this example, angles 1, 3, 5, and 7 measure 70°, and angles 2, 4, 6, and 8 measure 110°.

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