## Unit 7 Lesson 10: Estimating Proportions from Samples

### 1 Math Talk: Proportions (Warm up)

#### Student Task Statement

Mentally evaluate the proportion of chips that are blue.

17 are blue out of 50 chips

28 are blue out of 50 chips

17 are blue out of 20 chips

21 are blue out of 60 chips

### 2 Pass or Fail

#### Student Task Statement

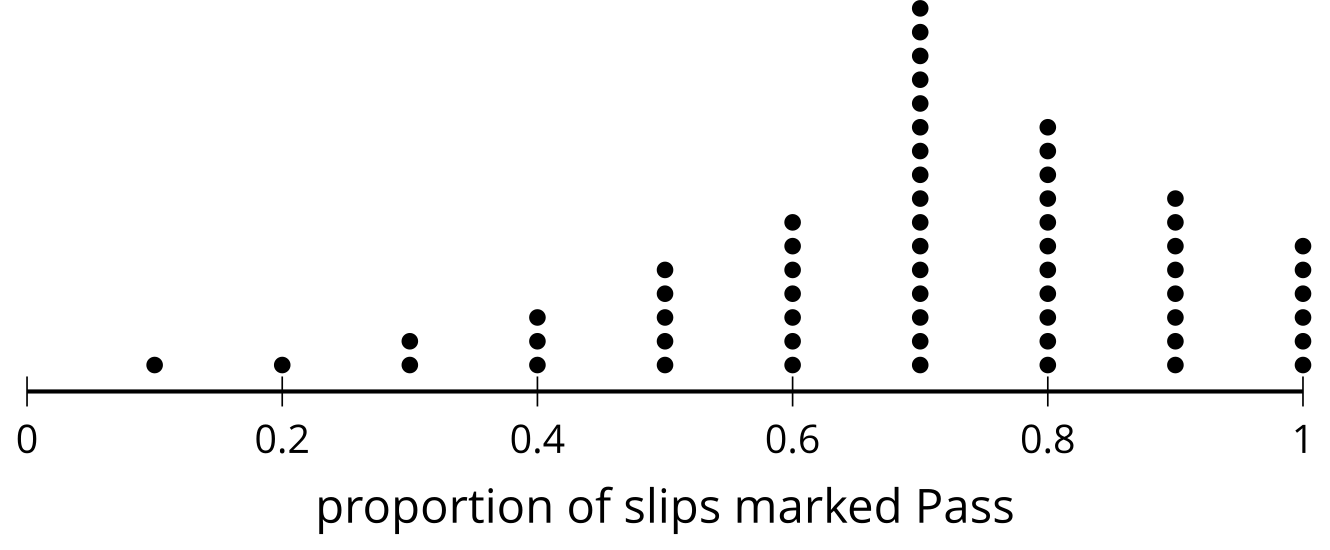
Your teacher will give you a bag with paper slips inside that are marked as either Pass or Fail. Do not empty the bag to look at all of the contents at once.

1. One partner should hold the bag so that the other partner cannot see inside while they draw a slip of paper. The other partner should draw 10 slips of paper from the bag, one at a time. After the 10 slips are drawn, record the number of slips marked Pass.
2. From the results of the first trial, estimate the proportion of the slips in the bag that are marked Pass.
3. Switch roles with your partner and repeat the process until you have run 5 trials. For each trial, compute the proportion of slips you drew that are marked Pass.

| * trial | * 1 | * 2 | * 3 | * 4 | * 5 |
| --- | --- | --- | --- | --- | --- |
| * number of Pass slips |  |  |  |  |  |
| * proportion of slips marked Pass |  |  |  |  |  |

1. Create a dot plot based on the trials from the class that shows the proportion of slips drawn that are marked Pass.
2. From the class dot plot, estimate the proportion of slips marked Pass in the bag. Explain your reasoning.

#### Activity Synthesis



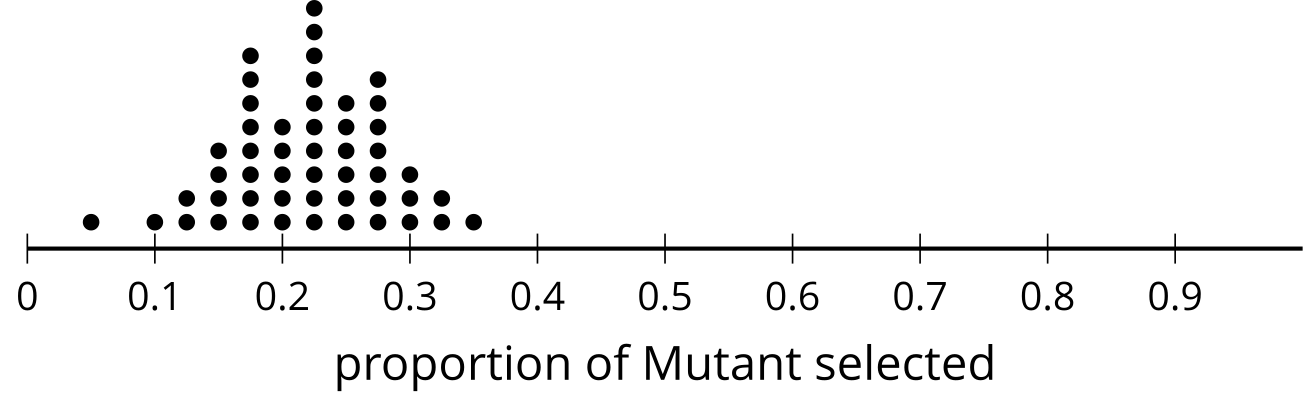
### 3 Fly Memory

#### Student Task Statement

A biologist is breeding fruit flies to include a specific genetic mutation that will be useful in understanding memory in humans. To check whether a fly has the mutation, a DNA sequence is analyzed in a way that kills the fly, so the biologist only wants to test a sample of the flies to estimate the proportion of flies that have the mutation.



The biologist selects 40 flies to sequence at random and finds that 9 of them have the genetic mutation.

1. Based on this sample, estimate the proportion of flies in this group that has the genetic mutation.
2. The scientist is worried that only having one sample may not be reliable for estimating the proportion of flies with the mutation, but does not want to sacrifice more flies to get a larger sample. The proportion from the sample is a good estimate for the population proportion, but it is difficult to understand the possible variability from a single value. Andre has a suggestion for how to better understand the variability:
   1. Assume the sample is representative of the population of flies and create a simulation that mimics what the scientist found. Andre gets 200 pieces of paper and marks 45 of them as Mutant and puts them all in a bag. Since Andre decided to use 200 pieces of paper, why should 45 of them be marked Mutant? What are some other combinations of total number of pieces of paper and number marked Mutant that he could use?
   2. Andre then simulates the scientist’s sample by drawing a slip of paper from the bag noting whether it is Mutant or not, then replacing the paper into the bag and drawing another paper until he has a sample of 40. He repeats this process for 50 trials and creates a dot plot showing the proportion that are Mutant from each trial. Estimate values on the dot plot a range of proportions that include about 95% of the proportions from the trials.
   * 
   1. Andre then finds the mean proportion from his simulations to be 0.2195 and the standard deviation to be 0.06. How far are your values from the last question from the mean? This will represent your estimated margin of error.
   2. Divide the distance from the last question by the standard deviation to get the margin of error in terms of the number of standard deviations.
3. Based on Andre’s simulations, should the scientist feel confident that the proportion of flies is within two standard deviations of the mean for the simulations?



© CC BY 2019 by Illustrative Mathematics®