Lesson 5: Coordinate Moves

Let's transform some figures and see what happens to the coordinates of points.

5.1: Translating Coordinates

Select all of the translations that take Triangle T to Triangle U. There may be more than one correct answer.



- 1. Translate (-3, 0) to (1, 2).
- 2. Translate (2, 1) to (-2, -1).
- 3. Translate (-4, -3) to (0, -1).
- 4. Translate (1, 2) to (2, 1).



5.2: Reflecting Points on the Coordinate Plane

On the **coordinate plane**:

- a. Plot each point and label each with its coordinates.
- b. Using the *x*-axis as the line of reflection, plot the image of each point.
- c. Label the image of each point with its coordinates.
- d. Include a label using a letter. For example, the image of point A should be labeled A'.
- 2. If the point (13, 10) were reflected using the *x*-axis as the line of reflection, what would be the coordinates of the image? What about (13, -20)? (13, 570)? Explain how you know.



- 3. The point R has coordinates (3, 2).
 - a. Without graphing, predict the coordinates of the image of point R if point R were reflected using the *y*-axis as the line of reflection.
 - b. Check your answer by finding the image of *R* on the graph.



- c. Label the image of point R as R'.
- d. What are the coordinates of R'?
- 4. Suppose you reflect a point using the *y*-axis as line of reflection. How would you describe its image?



5.3: Transformations of a Segment

Apply each of the following transformations to segment *AB*.

- 1. Rotate segment *AB* 90 degrees counterclockwise around center *B*. Label the image of *A* as *C*. What are the coordinates of *C*?
- 2. Rotate segment AB 90 degrees counterclockwise around center A. Label the image of B as D. What are the coordinates of D?
- 3. Rotate segment AB 90 degrees clockwise around (0, 0). Label the image of A as E and the image of B as F. What are the coordinates of E and F?
- 4. Compare the two 90-degree counterclockwise rotations of segment *AB*. What is the same about the images of these rotations? What is different?

Are you ready for more?

Suppose EF and GH are line segments of the same length. Describe a sequence of transformations that moves EF to GH.

Lesson 5 Summary

We can use coordinates to describe points and find patterns in the coordinates of transformed points.

We can describe a translation by expressing it as a sequence of horizontal and vertical translations. For example, segment AB is translated right 3 and down 2.



Reflecting a point across an axis changes the sign of one coordinate. For example, reflecting the point A whose coordinates are (2, -1) across the x-axis changes the sign of the y-coordinate, making its image the point A' whose coordinates are (2, 1). Reflecting the point A across the y-axis changes the sign of the x-coordinate, making the image the point A'' whose coordinates are (-2, -1).

		У/ —2						
		1	 	A' =	(2,	1)		
-3	- 2 -1	0		2 3	3 2	4 <u>y</u>	5 1	x
-3 A" =	-2 -1 (-2, -1	0 -1 1) -2		2 3 A =	3 ² (2, -	4 <u>:</u> 1)	5 1	x

Reflections across other lines are more complex to describe.



We don't have the tools yet to describe rotations in terms of coordinates in general. Here is an example of a 90° rotation with center (0, 0) in a counterclockwise direction.



Point *A* has coordinates (0, 0). Segment *AB* was rotated 90° counterclockwise around *A*. Point *B* with coordinates (2, 3) rotates to point *B*' whose coordinates are (-3, 2).