

Lesson 22: Volume As a Function of . . .

Let's compare water heights in different containers.

22.1: Missing Information?

A cylinder and sphere have the same height.

1. If the sphere has a volume of 36π cubic units, what is the height of the cylinder?
2. What is a possible volume for the cylinder? Be prepared to explain your reasoning.

22.2: Scaling Volume of a Sphere

1. Fill in the missing volumes in terms of π . Add two more radius and volume pairs of your choosing.

radius	1	2	3	$\frac{1}{2}$	$\frac{1}{3}$	100			r
volume	$\frac{4}{3}\pi$								

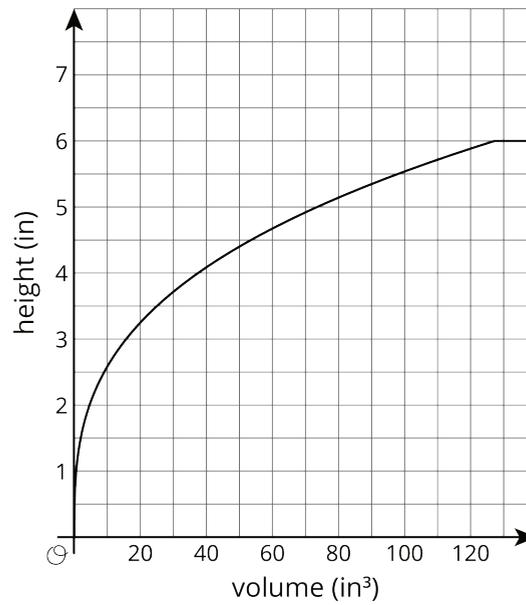
- a. How does the volume of a sphere with radius 2 cm compare to the volume of a sphere with radius 1 cm?
 - b. How does the volume of a sphere with radius $\frac{1}{2}$ cm compare to the volume of a sphere with radius 1 cm?
2. A sphere has a radius of length r .
 - a. What happens to the volume of this sphere if its radius is doubled?
 - b. What happens to the volume of this sphere if its radius is halved?
 3. Sphere Q has a volume of 500 cm^3 . Sphere S has a radius $\frac{1}{5}$ as large as Sphere Q. What is the volume of Sphere S?

22.3: A Cylinder, a Cone, and a Sphere

Three containers of the same height were filled with water at the same rate. One container is a cylinder, one is a cone, and one is a sphere. As they were filled, the relationship between the volume of water and the height of the water was recorded in different ways, shown here:

- Cylinder: $h = \frac{V}{4\pi}$

- Cone:



- Sphere:

volume (in ³)	height (in)
0	0
8.38	1
29.32	2
56.55	3
83.76	4
104.72	5
113.04	6
120	6
200	6

1. The maximum volume of water the cylinder can hold is 24π . What is the radius of the cylinder?

2. Graph the relationship between the volume of water poured into the cylinder and the height of water in the cylinder on the same axes as the cone. What does the slope of this line represent?

