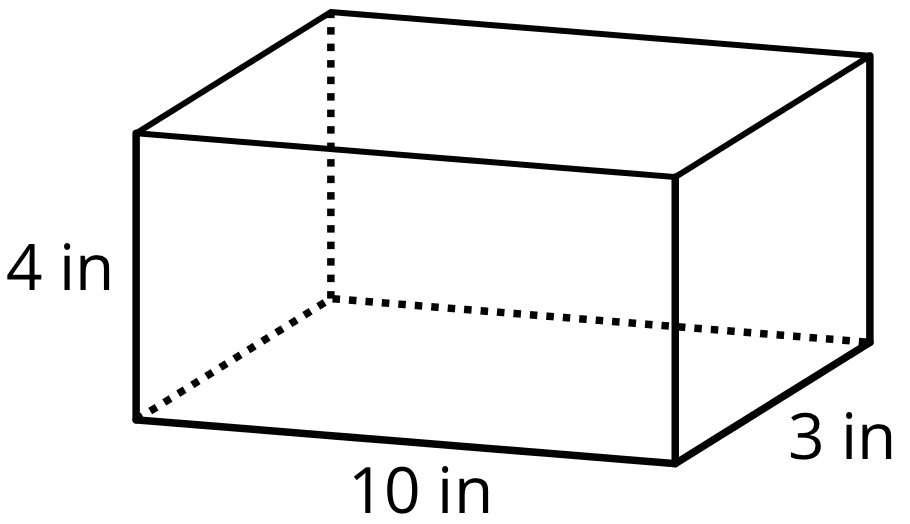
## Lesson 11: Volume of Prisms

Let’s look at the volume of prisms that have fractional measurements.

### 11.1: A Box of Cubes

1. How many cubes with an edge length of 1 inch fill this box?

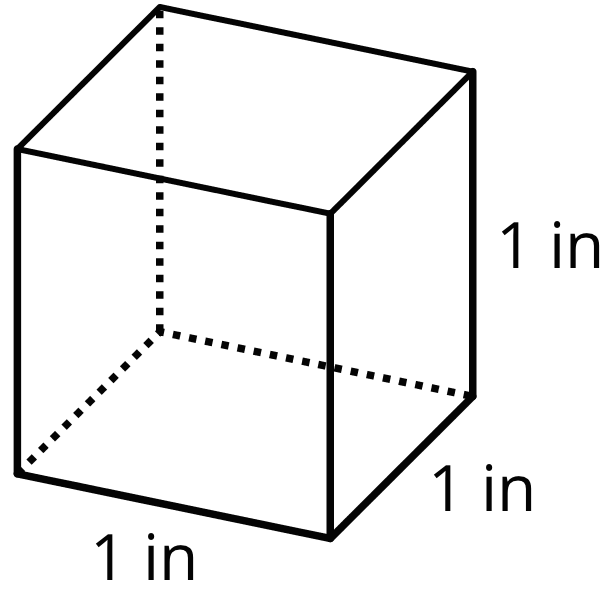
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1. If the cubes had an edge length of 2 inches, would you need more or fewer cubes to fill the box? Explain your reasoning.
2. If the cubes had an edge length of  inch, would you need more or fewer cubes to fill the box? Explain your reasoning.

### 11.2: Volumes of Cubes and Prisms

Your teacher will give you cubes that have edge lengths of inch.

1. Here is a drawing of a cube with edge lengths of 1 inch.

* 
  1. How many cubes with edge lengths of inch are needed to fill this cube?
  2. What is the volume, in cubic inches, of a cube with edge lengths of inch? Explain or show your reasoning.

1. Four cubes are piled in a single stack to make a prism. Each cube has an edge length of inch. Sketch the prism, and find its volume in cubic inches.
2. Use cubes with an edge length of inch to build prisms with the lengths, widths, and heights shown in the table.
   1. For each prism, record in the table how many -inch cubes can be packed into the prism and the volume of the prism.

| * + prism length (in) | * + prism width (in) | * + prism height (in) | * + number of -inch cubes in prism | * + volume of prism (in3) |
| --- | --- | --- | --- | --- |
|  |  |  |  |  |
| * + 1 | * + 1 |  |  |  |
| * + 2 | * + 1 |  |  |  |
| * + 2 | * + 2 | * + 1 |  |  |
| * + 4 | * + 2 |  |  |  |
| * + 5 | * + 4 | * + 2 |  |  |
| * + 5 | * + 4 |  |  |  |

* 1. Examine the values in the table. What do you notice about the relationship between the edge lengths of each prism and its volume?

1. What is the volume of a rectangular prism that is inches by inches by 4 inches? Show your reasoning.

#### Are you ready for more?

A unit fraction has a 1 in the numerator.

* These are unit fractions: .
* These are *not* unit fractions: .

1. Find three unit fractions whose sum is . An example is:  How many examples like this can you find?
2. Find a box whose surface area in square units equals its volume in cubic units. How many like this can you find?

### 11.3: Cubes with Fractional Edge Lengths

1. Diego says that 108 cubes with an edge length of inch are needed to fill a rectangular prism that is 3 inches by 1 inch by inch.
   1. Explain or show how this is true. If you get stuck, consider drawing a diagram.
   2. What is the volume, in cubic inches, of the rectangular prism? Explain or show your reasoning.
2. Lin and Noah are packing small cubes into a larger cube with an edge length of inches. Lin is using cubes with an edge length of inch, and Noah is using cubes with an edge length of inch.
   1. Who would need more cubes to fill the -inch cube? Be prepared to explain your reasoning.
   2. If Lin and Noah each use their small cubes to find the volume of the larger -inch cube, will they get the same answer? Explain or show your reasoning.

### 11.4: Fish Tank and Baking Pan

1. A nature center has a fish tank in the shape of a rectangular prism. The tank is 10 feet long, feet wide, and 6 feet tall.
   1. What is the volume of the tank in cubic feet? Explain or show your reasoning.
   * 
   1. The nature center's caretaker filled of the tank with water. What was the volume of the water in the tank, in cubic feet? What was the height of the water in the tank? Explain or show your reasoning.
   2. Another day, the tank was filled with 330 cubic feet of water. The height of the water was what fraction of the height of the tank? Show your reasoning.
2. Clare’s recipe for banana bread won’t fit in her favorite pan. The pan is inches by 11 inches by 2 inches. The batter fills the pan to the very top, and when baking, the batter spills over the sides. To avoid spills, there should be about an inch between the top of the batter and the rim of the pan.

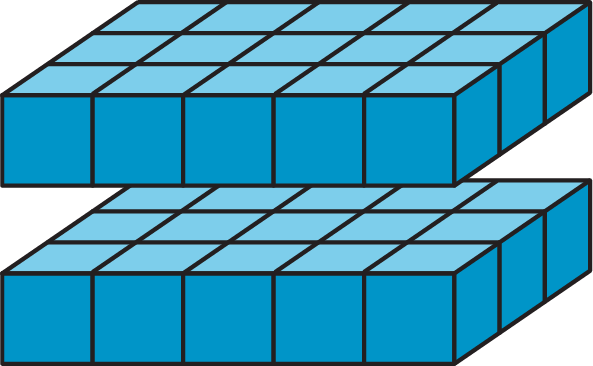
* Clare has another pan that is 9 inches by 9 inches by inches. If she uses this pan, will the batter spill over during baking?

#### Are you ready for more?

1. Find the area of a rectangle with side lengths and .
2. Find the volume of a rectangular prism with side lengths , , and .
3. What do you think happens if we keep multiplying fractions ?
4. Find the area of a rectangle with side lengths and .
5. Find the volume of a rectangular prism with side lengths , , and .
6. What do you think happens if we keep multiplying fractions ?

### Lesson 11 Summary

If a rectangular prism has edge lengths of 2 units, 3 units, and 5 units, we can think of it as 2 layers of unit cubes, with each layer having unit cubes in it. So the volume, in cubic units, is:



To find the volume of a rectangular prism with fractional edge lengths, we can think of it as being built of cubes that have a unit fraction for their edge length. For instance, if we build a prism that is -inch tall, -inch wide, and 4 inches long using cubes with a -inch edge length, we would have:

* A height of 1 cube, because .
* A width of 3 cubes, because .
* A length of 8 cubes, because .

The volume of the prism would be , or 24 cubic units. How do we find its volume in cubic inches? We know that each cube with a -inch edge length has a volume of cubic inch, because . Since the prism is built using 24 of these cubes, its volume, in cubic inches, would then be , or 3 cubic inches.

The volume of the prism, in cubic inches, can also be found by multiplying the fractional edge lengths in inches: ​​​​​​

If a rectangular prism has edge lengths units, units, and units, the volume is the product of , , and .

This means that if we know the *volume* and *two edge lengths*, we can divide to find the *third* edge length.

Suppose the volume of a rectangular prism is cm3, one edge length is cm, another is cm, and the third edge length is unknown. We can write a multiplication equation to represent the situation:

We can find the third edge length by dividing:



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