## Lesson 9: Solving Quadratic Equations by Using Factored Form

* Let’s solve some quadratic equations that before now we could only solve by graphing.

### 9.1: Why Would You Do That?

Let's try to find at least one solution to .

1. Choose a whole number between 0 and 10.
2. Evaluate the expression , using your number for .
3. If your number doesn't give a value of 0, look for someone in your class who may have chosen a number that does make the expression equal 0. Which number is it?
4. There is another number that would make the expression equal 0. Can you find it?

### 9.2: Let’s Solve Some Equations!

1. To solve the equation , Tyler wrote out the following steps. Analyze Tyler’s work. Write down what Tyler did in each step.



1. Solve each equation by rewriting it in factored form and using the zero product property. Show your reasoning.

#### Are you ready for more?

Solve this equation and explain or show your reasoning.

### 9.3: Revisiting Quadratic Equations with Only One Solution

1. The other day, we saw that a quadratic equation can have 0, 1, or 2 solutions. Sketch graphs that represent three quadratic functions: one that has no zeros, one with 1 zero, and one with 2 zeros.
2. Use graphing technology to graph the function defined by . What do you notice about the -intercepts of the graph? What do the -intercepts reveal about the function?
3. Solve by using the factored form and zero product property. Show your reasoning. What solutions do you get?
4. Write an equation to represent another quadratic function that you think will only have one zero. Graph it to check your prediction.

### Lesson 9 Summary

Recently, we learned strategies for transforming expressions from standard form to factored form. In earlier lessons, we have also seen that when a quadratic expression is in factored form, it is pretty easy to find values of the variable that make the expression equal zero. Suppose we are solving the equation , which says that the product of and is 0. By the zero product property, we know this means that either or , which then tells us that 0 and -4 are solutions.

Together, these two skills—writing quadratic expressions in factored form and using the zero product property when a factored expression equals 0—allow us to solve quadratic equations given in other forms. Here is an example:

When a quadratic equation is written as , we can also see the number of solutions the equation has.

In the example earlier, it was not obvious how many solutions there would be when the equation was . When the equation was rewritten as , we could see that there were two numbers that could make the expression equal 0: 14 and -10.

How many solutions does the equation have?

Let’s rewrite it in factored form: . The two factors are identical, which means that there is only one value of that makes the expression equal 0. The equation has only one solution: 10.



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